



# Post-inflationary axion dark matter search with a dielectric haloscope

Axions beyond Gen 2, Jan 28<sup>th</sup> 2021

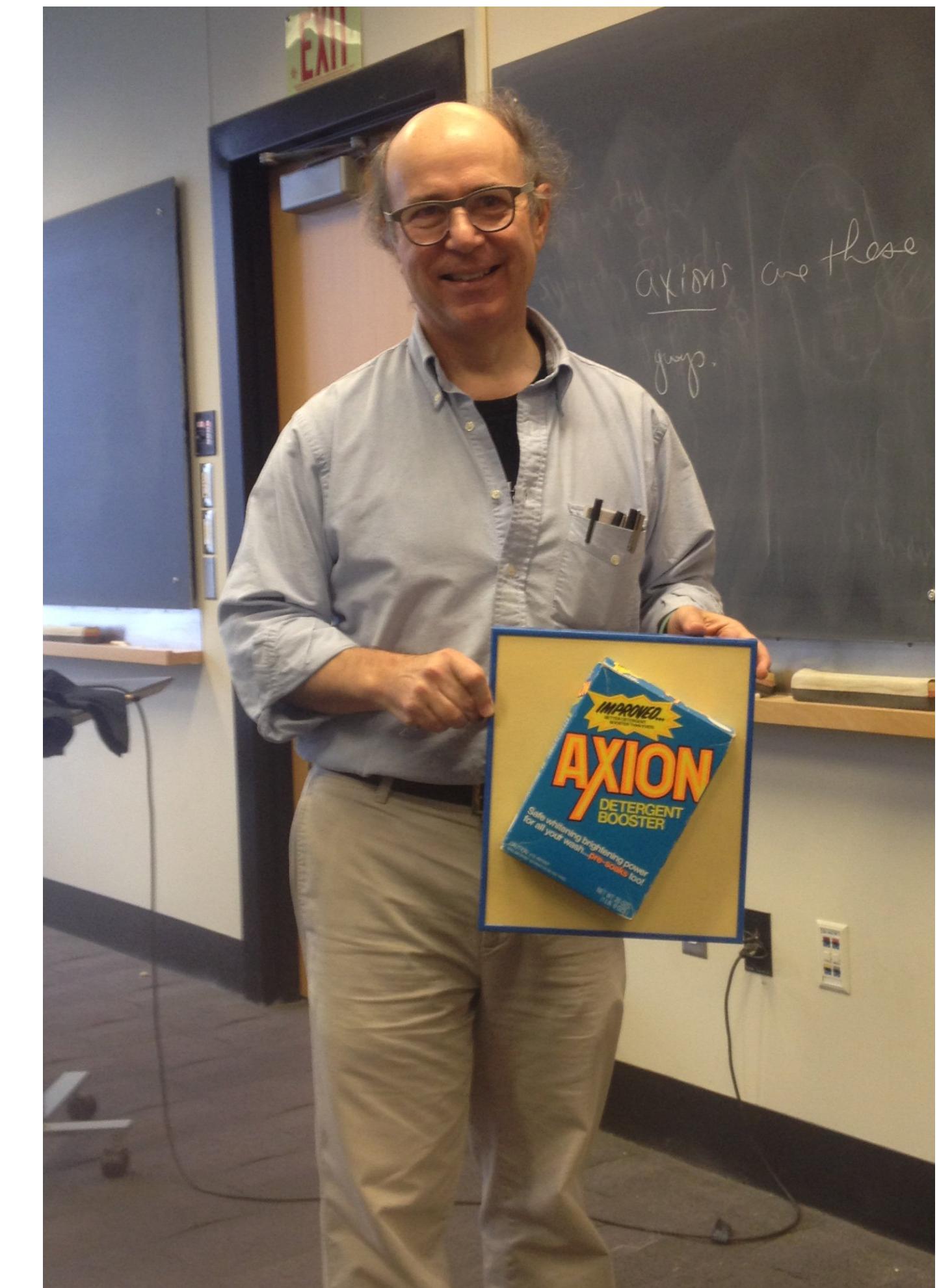
Chang Lee

MAX-PLANCK-INSTITUT  
FÜR PHYSIK



# Overview

- Theoretical motivations
- Scale-up & challenges
- Dielectric haloscope
- MADMAX experiment
- Proof-of-principle setup:  
100mm setup in LHe
- Conclusion



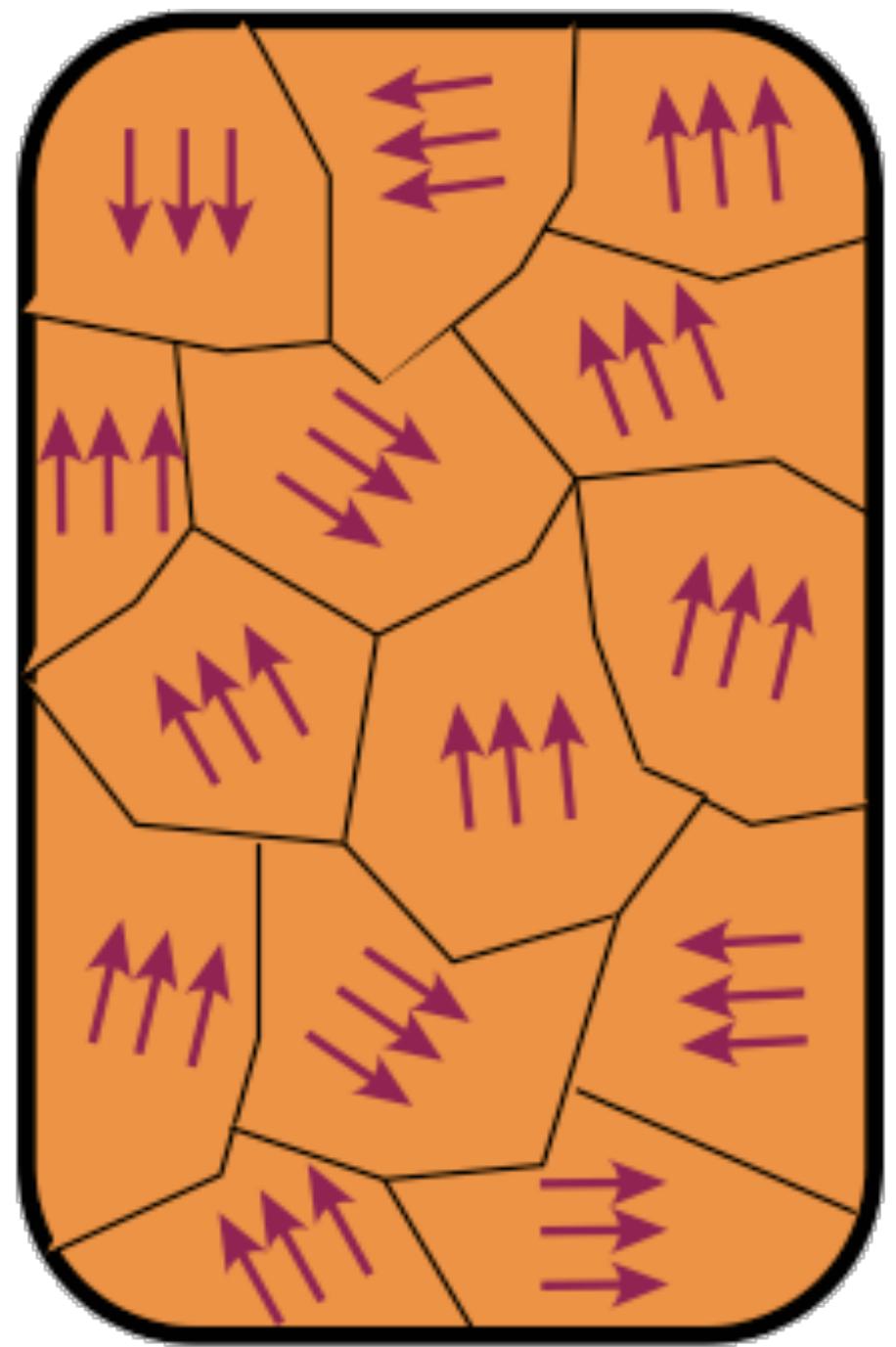
“The box is empty... OR IS IT?”

from Twitter@FrankWilczek

# Post-inflation scenario

*“Terra incognita”*

<http://physicstuff.com/how-do-magnets-work/>



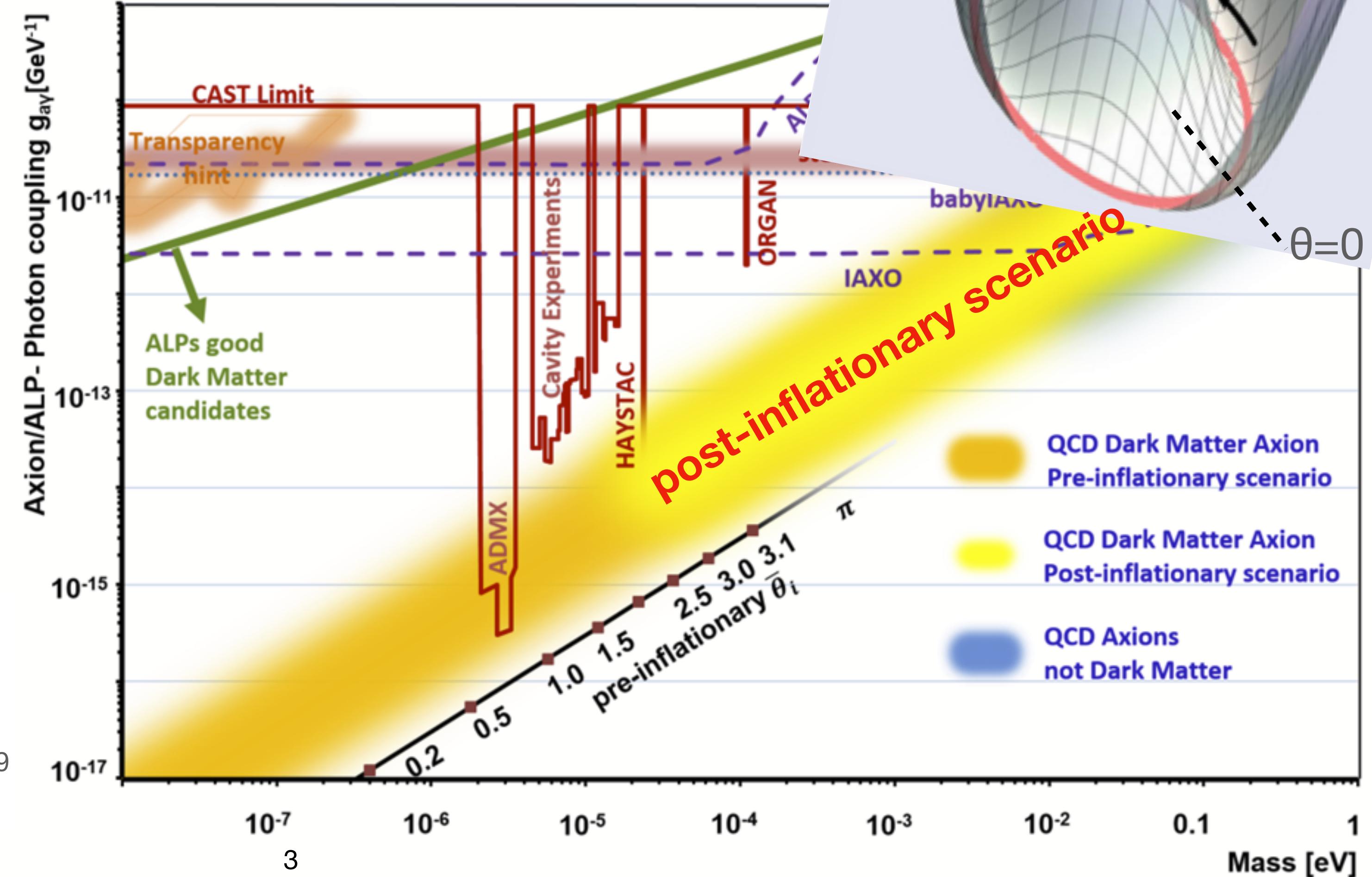
M. Kawasaki et al., Phys. Rev. D 91, 065014 (2015)

T. Hiramatsu, et al., Phys. Rev. D 85, 105020 (2012)

S. Borsanyi, et al., Nature 539, 69 (2016)

V. B. Klaer and G. D. Moore, J. Cosmol. Astropart. Phys. 2017 (11), 049

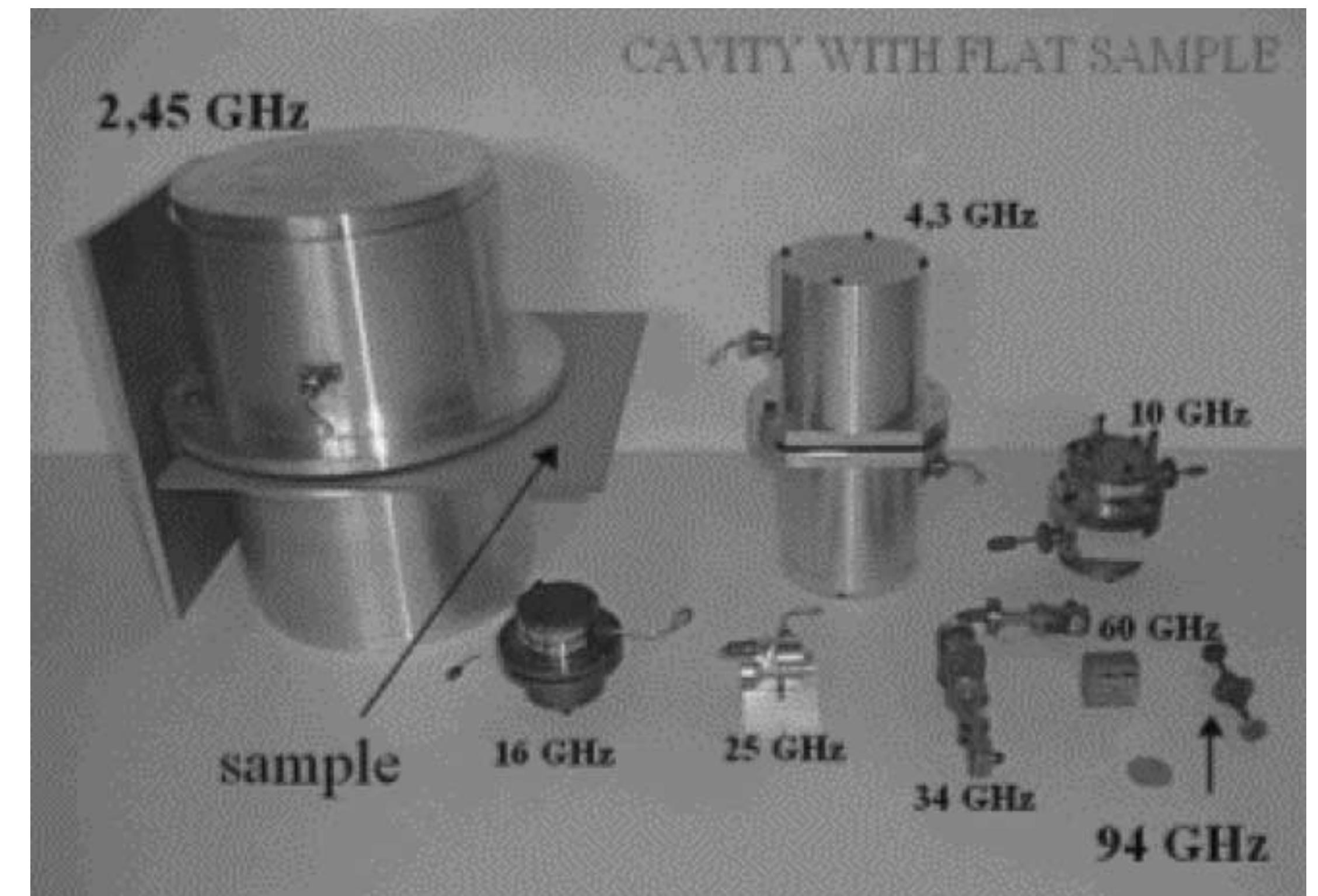
R. T. Co, et al., Phys. Rev. Lett. 124, 251802 (2020)



# High frequency challenge

## How to be sensitive above 10 GHz

- $P_{\text{sig}} \propto QV$ .
- Single-mode resonator shrinks rapidly at high frequency.
- Q also decreases with higher skin loss
- How to reach QCD above 10 GHz?



1 GHz cavity



image from Wikipedia: O'zapft is!

10 GHz cavity

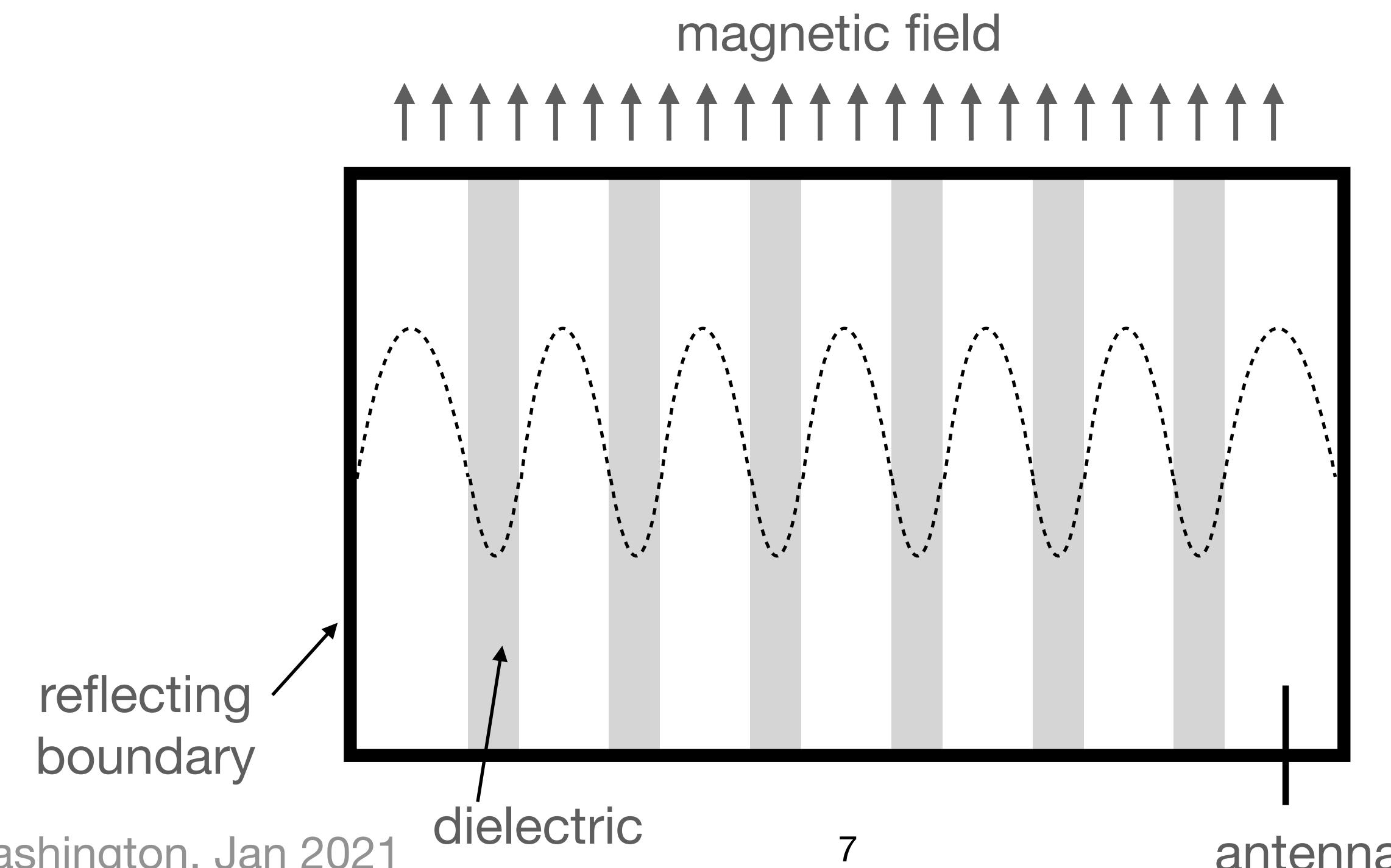
# Scale-up & challenges



<https://abeautifulmess.com/how-to-build-a-champagne-tower/>

# Dielectric-loaded resonator

- Resonant cavity loaded with dielectric to maximize overlap with  $E_a$ .
  - Concept already used by ORPHEUS and ORGAN.

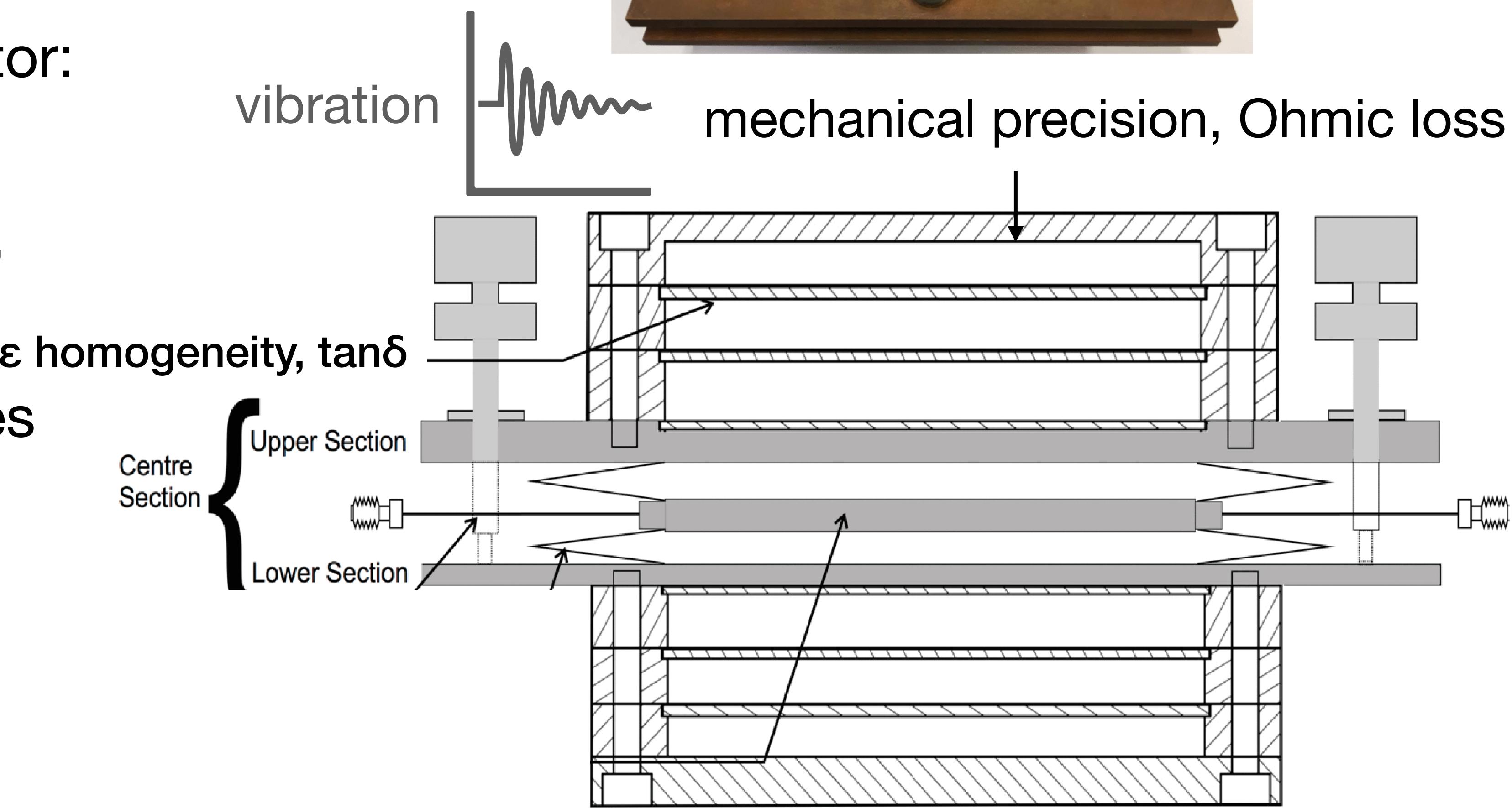
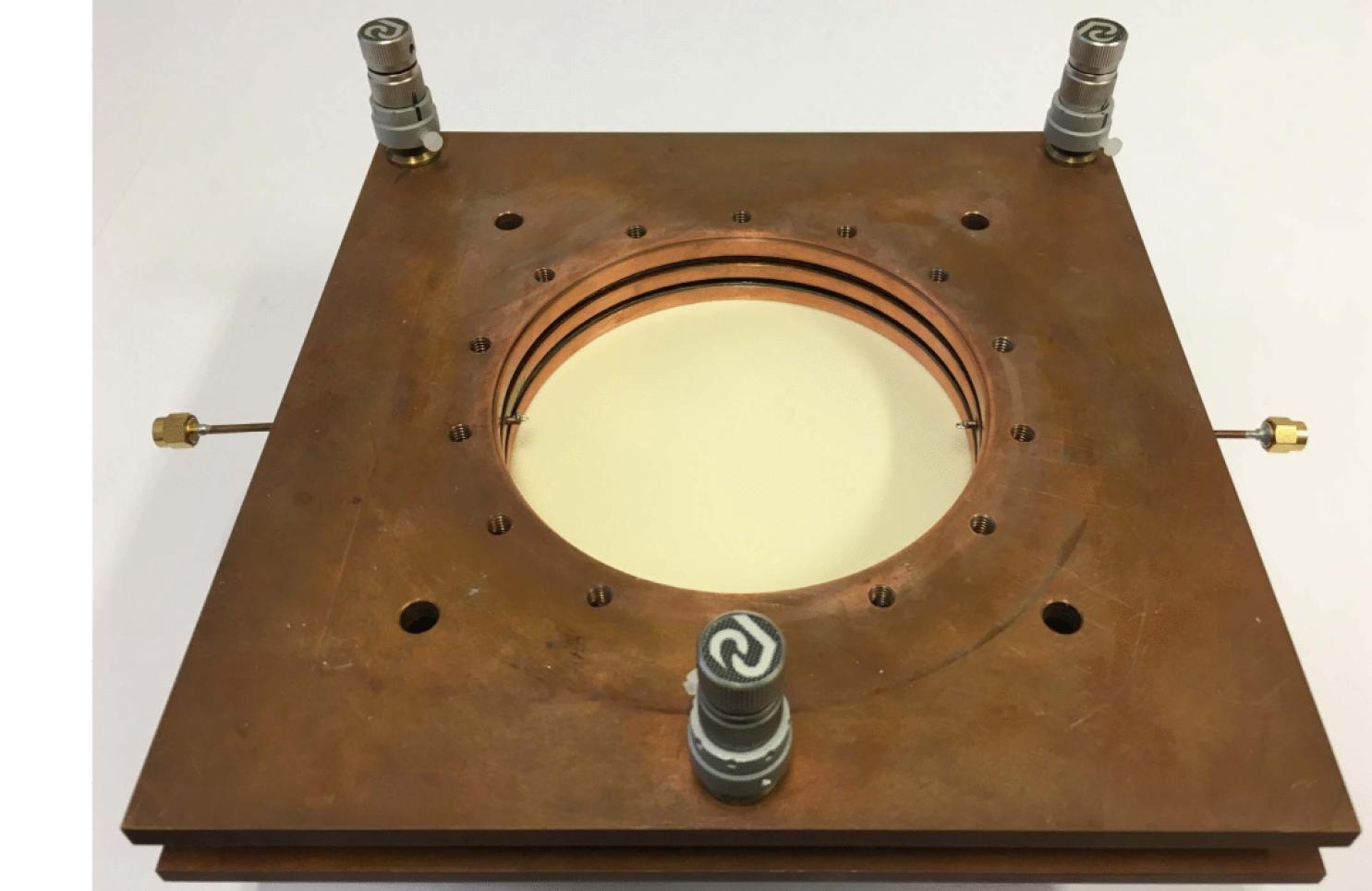


ORPHEUS: 3rd Workshop on Microwave Cavities  
and Detectors for Axion Research, Aug. 2018 LLNL,  
ORGAN: arXiv:1706.00209

# Increasing Q-factor

## Quality front

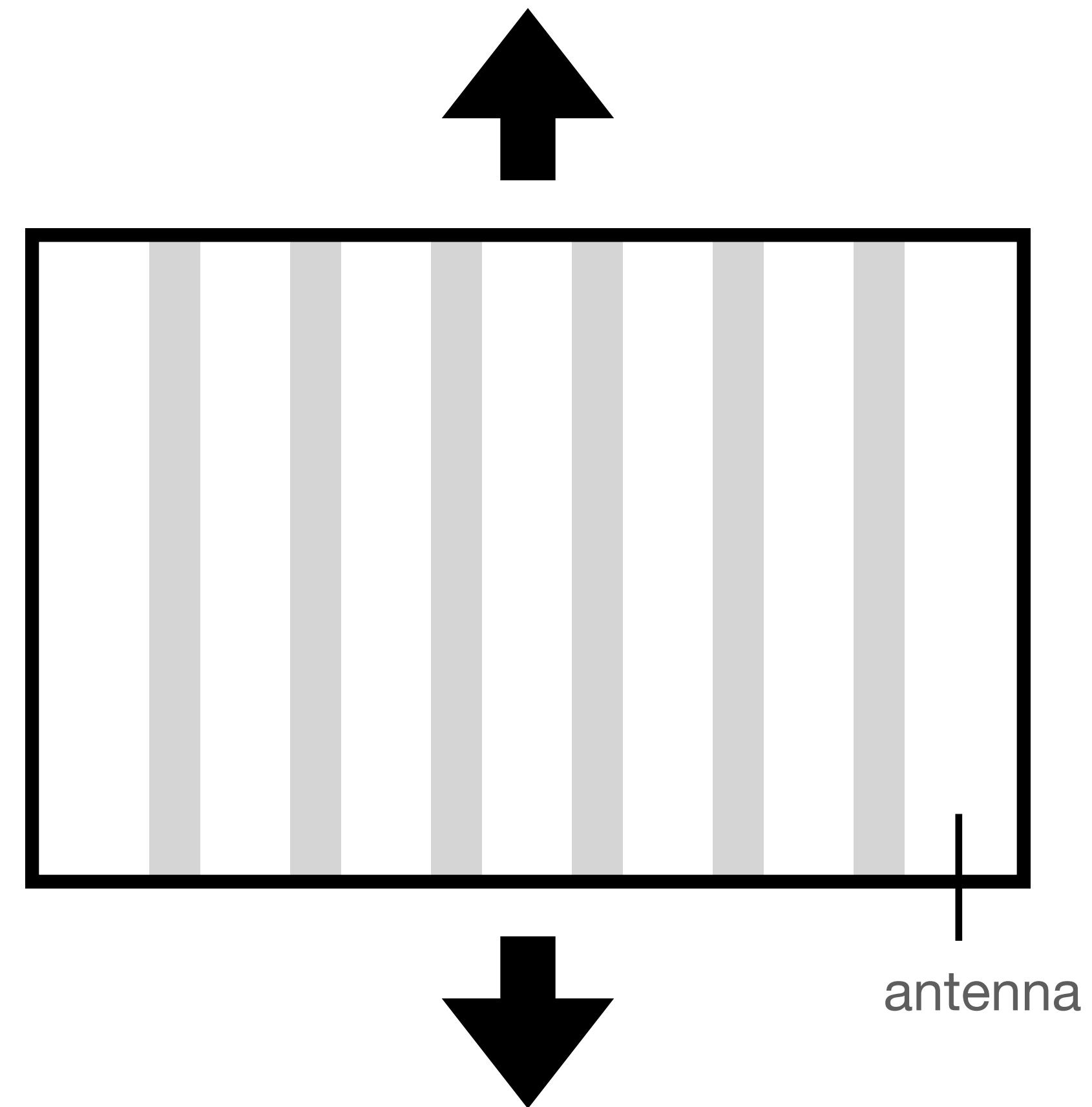
- Example: Bragg resonator:  
 $Q_0 \sim 100k$  @ TE01
- $Q > 100k$  is challenging,  
especially with
  - complicated structures
  - cryogenic temp
  - Tuning



J. Bale et al., *IEEE Trans. Ultrason., Ferroelectr., and Freq Control*, vol. 65, pp. 281, 2018

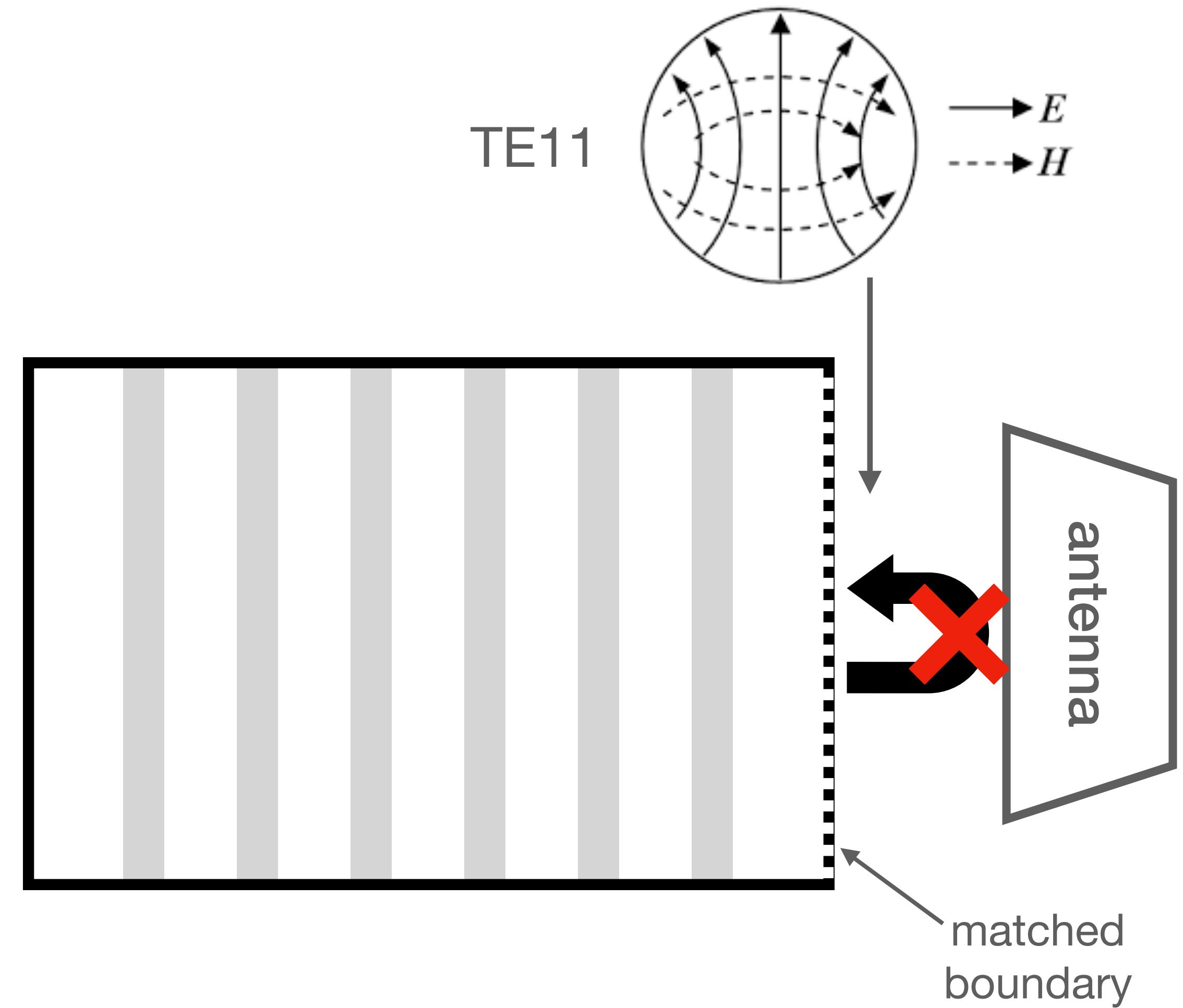
# Increasing volume

- Large volume: large magnet & cryostat
  - Expensive, but solutions exist
- Increase the transverse dimension:
  - Over-moded system:  
Mode-crowding, mode-crossing loss,  
coupling ambiguity



# Increasing volume longitudinal dimensions

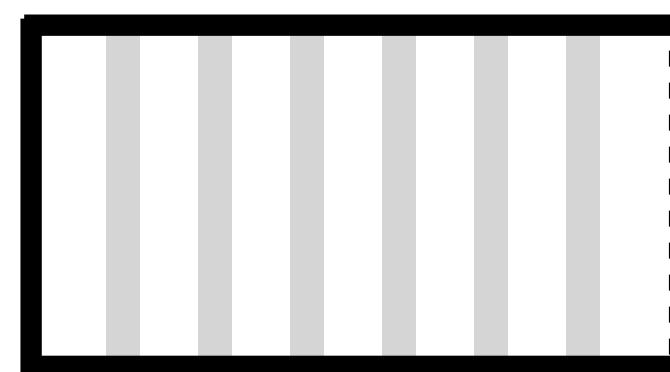
- Matched boundary (antenna, taper):
  - No longitudinal modes
  - Detect **Traveling wave** instead of standing wave modes.
  - Lower Q (or boost factor), but Q increases with many disks
- Reflected beam  $\neq$  axion induced beam



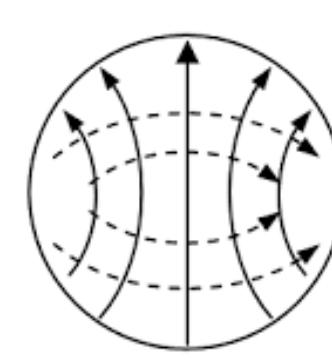
# Without lateral walls

“open” system

1. less mode-crowding



“closed”  
system



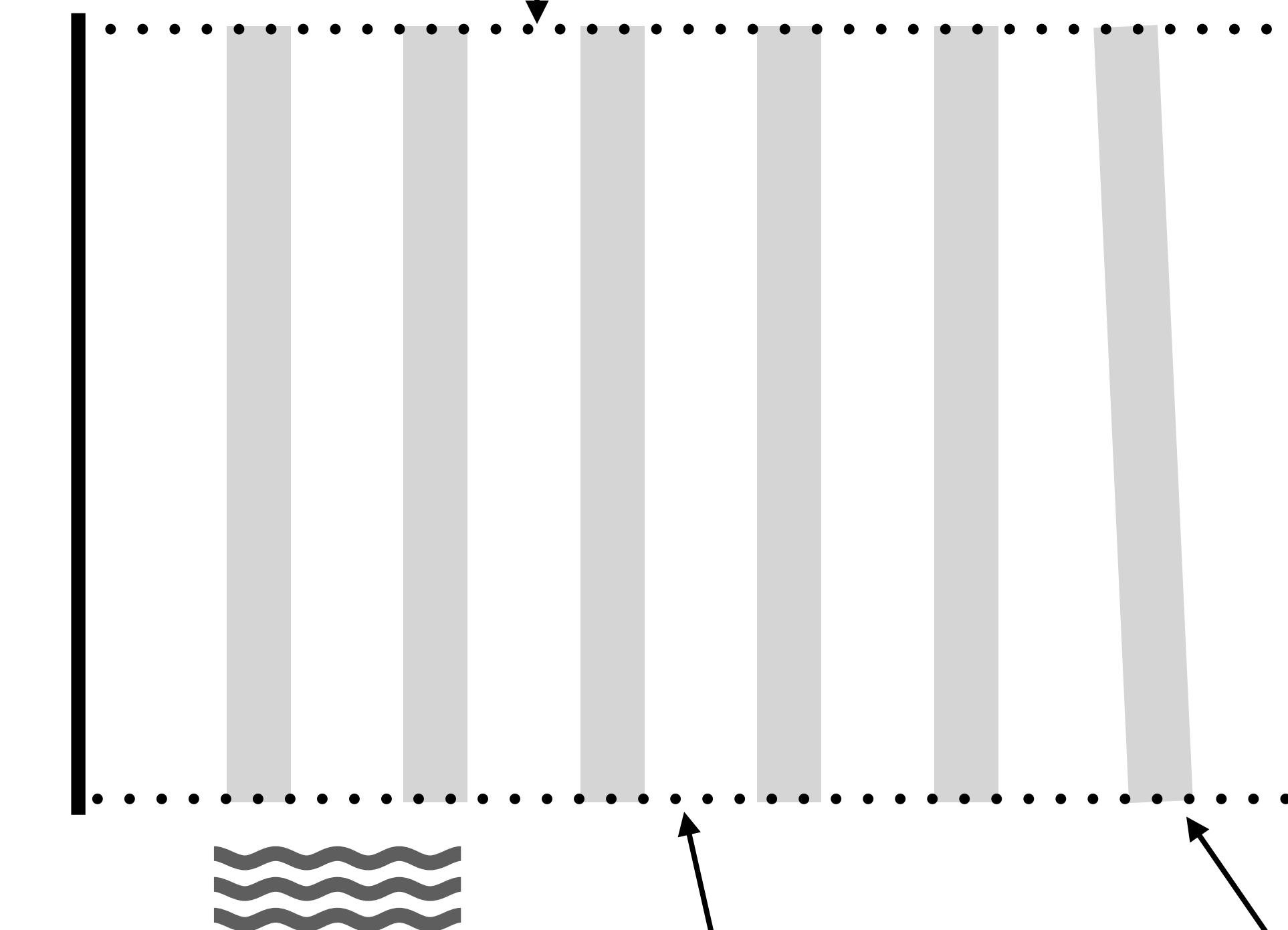
TE11

B. radiation loss  
on sides

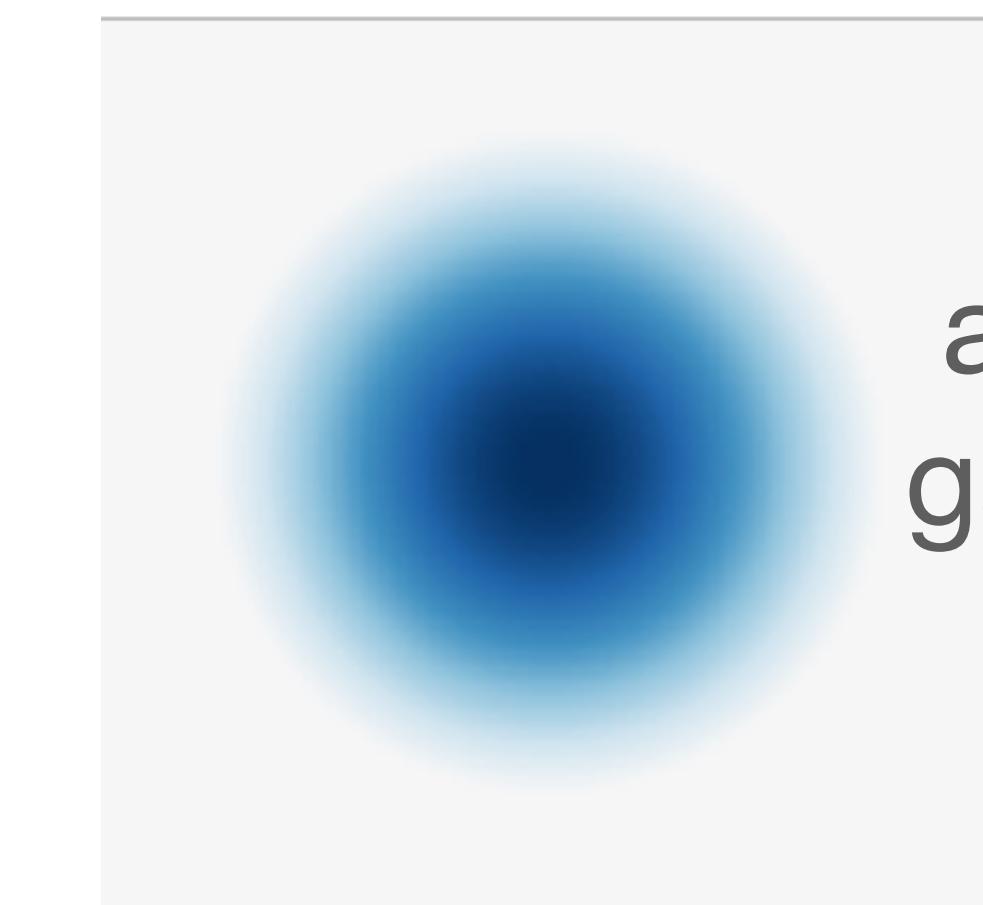
2. no Ohmic loss



A. radiation loss via  
surface current



3. diffraction loss  $\rightarrow 0$   
for  $R \gg \lambda$  or curved mirror



approx.  
gaussian  
beam

C.  $Z, k_{\text{trans}}?$   
ex) reflection off cryostat

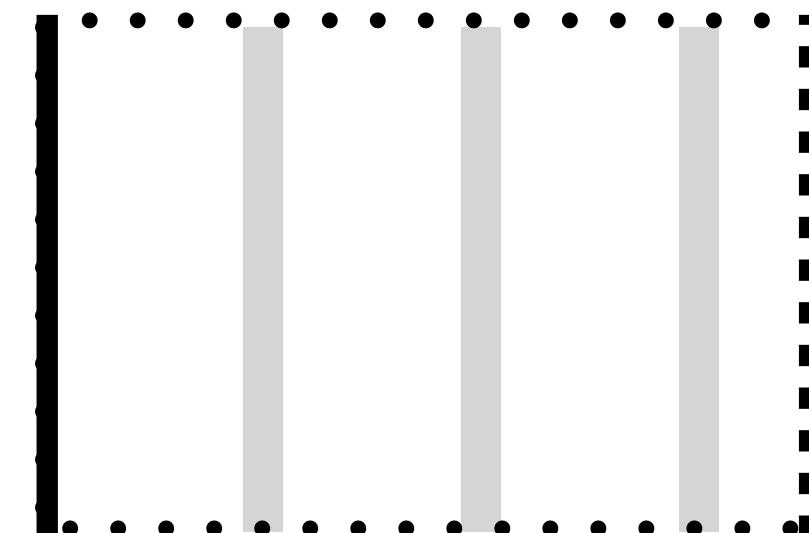
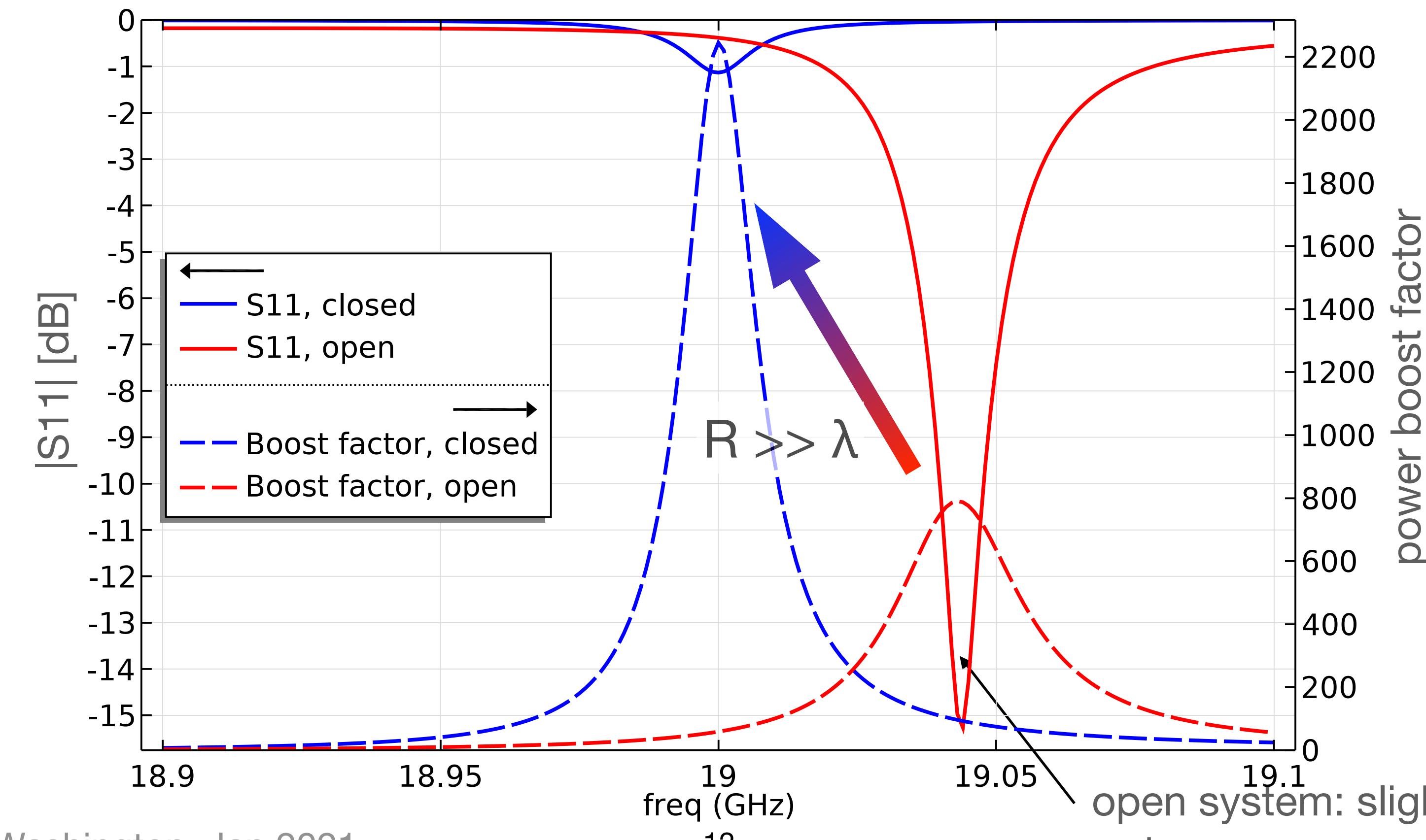
D. misalignment

# Open vs. closed systems

- Example: simulation of  $3 \times \phi 100\text{mm}$  sapphire disks tuned @ 19 GHz.

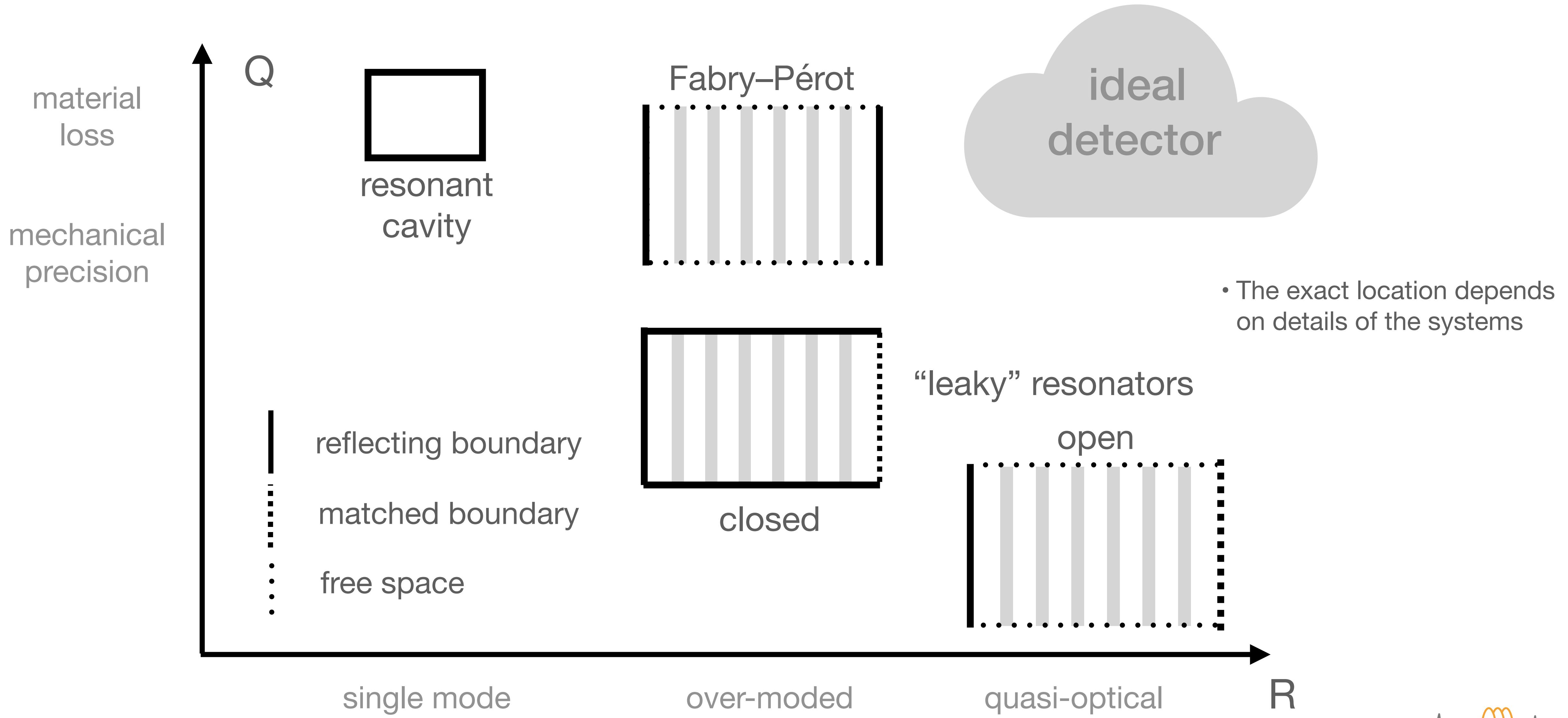


closed



open

# Scale-up challenges overview

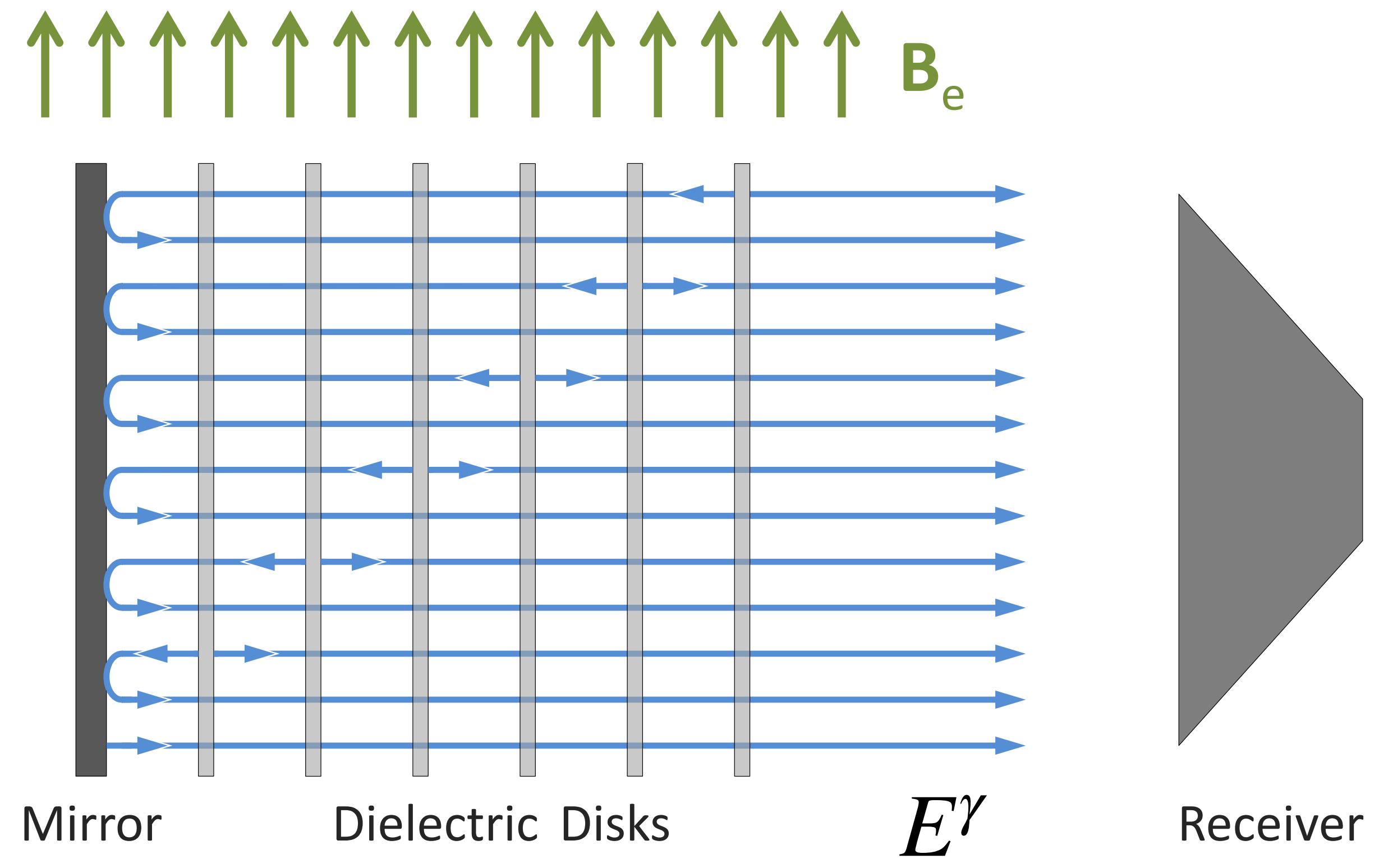


# Dielectric haloscope

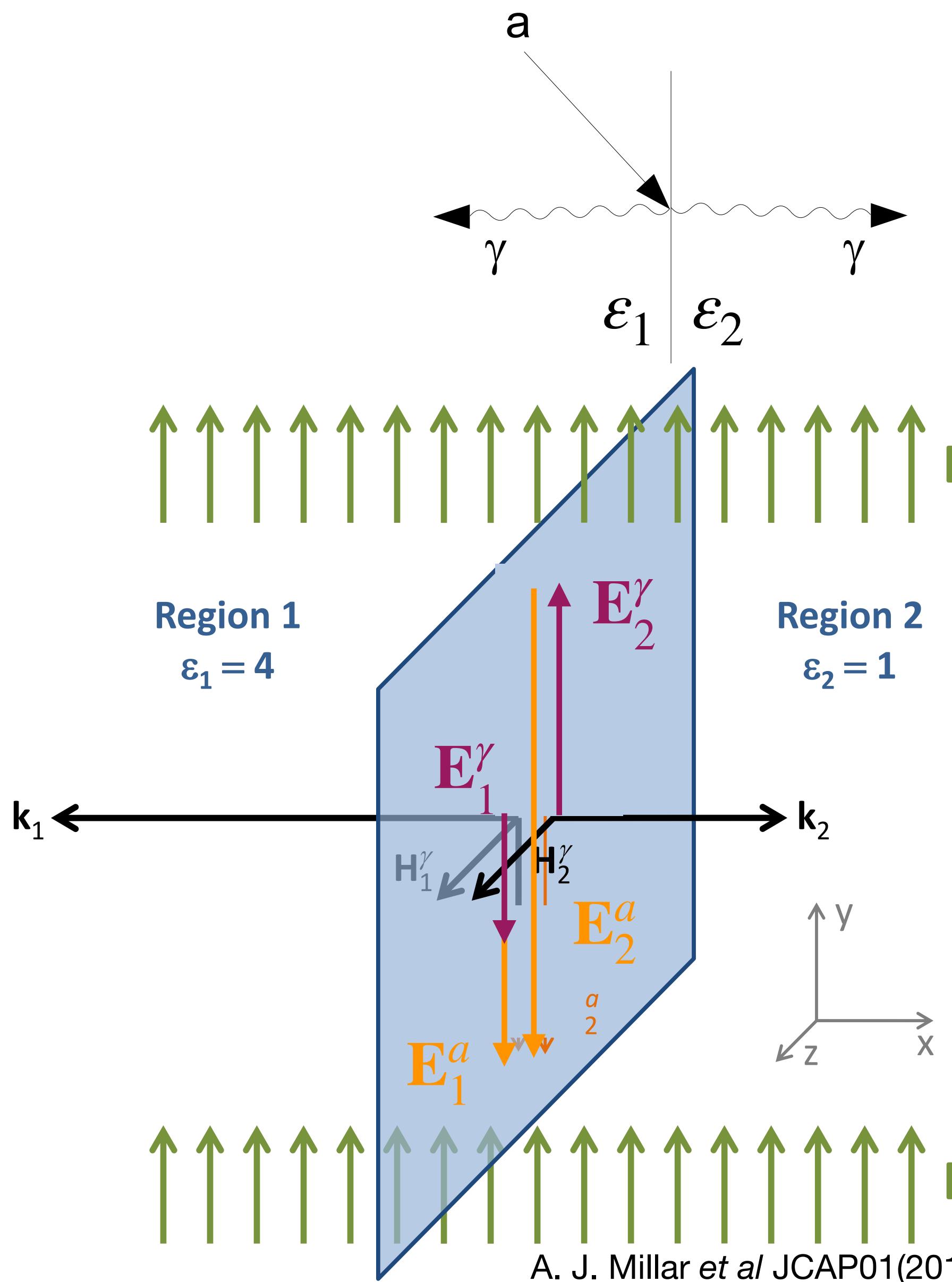
# Dielectric haloscope

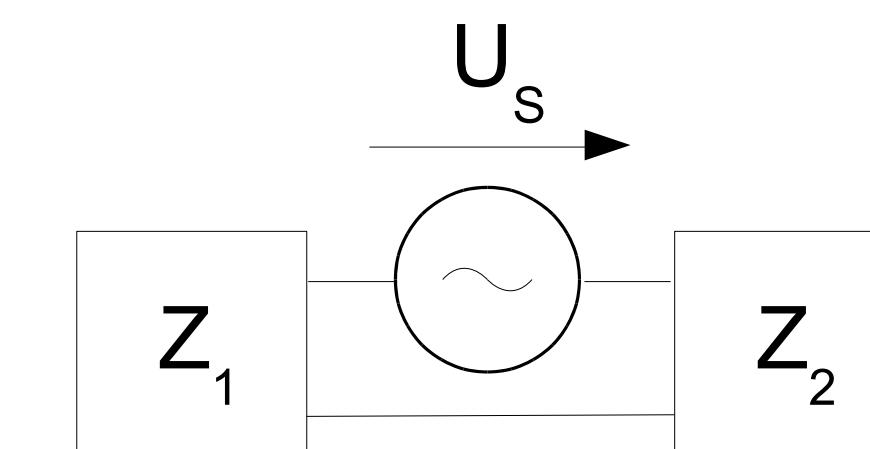
A. Caldwell, et al., *PRL*, 118(9), 091801.

- Large, over-moded, **leaky resonator**
  - **Matched boundary** on one end.  
Open / closed boundary on sides
- Boost factor:  $\beta = \frac{E^\gamma}{E_0}$ .
- $P_{\text{sig}} \propto \beta^2 A$   
(equivalent to  $QV$  for cavities).



# Axion-induced traveling wave



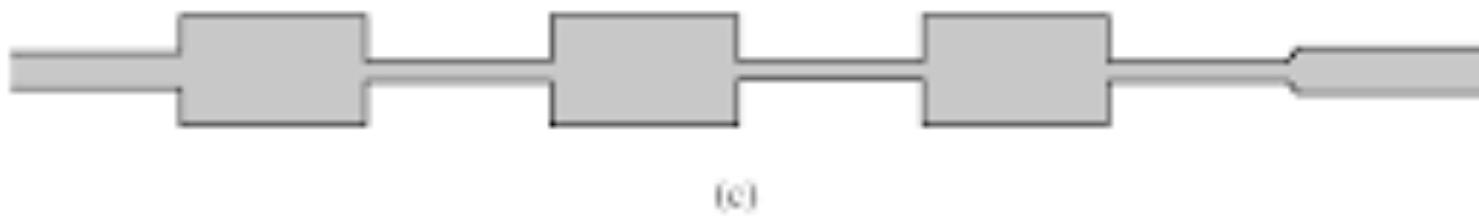
- = 
- $E_{1,2}^\alpha = -\frac{g_{a\gamma}B_e}{\epsilon_{1,2}}a$
- $E_1^\gamma = \frac{Z_1}{Z_1 + Z_2} (E_2^\alpha - E_1^\alpha)$  (traveling wave)
  - voltage divider!
  - characteristic impedance
- Modify  $Z$  to increase the radiation?

# Disk spacing

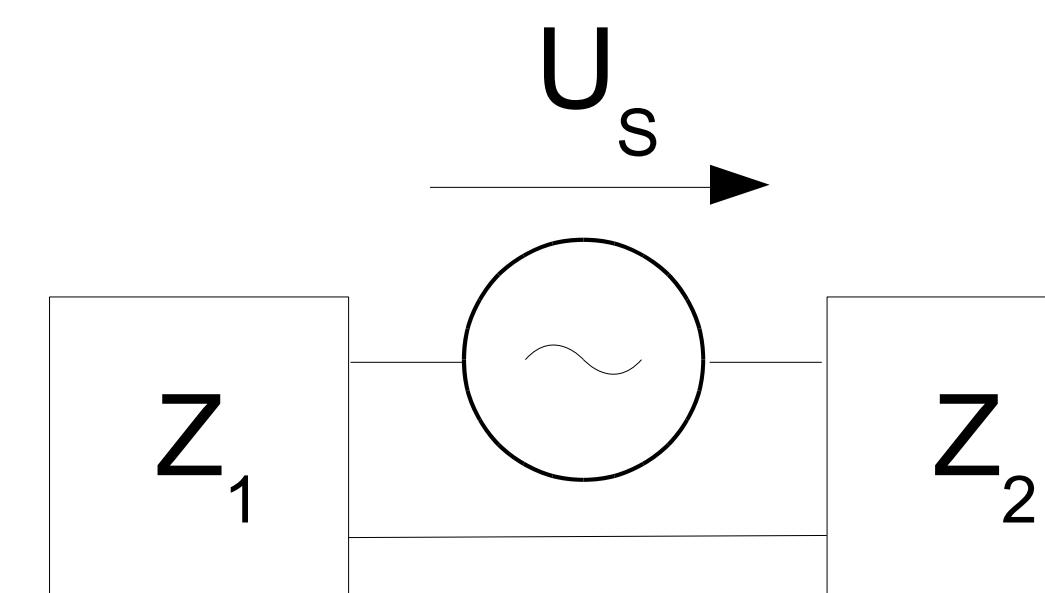
## Resonant case

- Maximize the axion-induced radiation from the metal surface

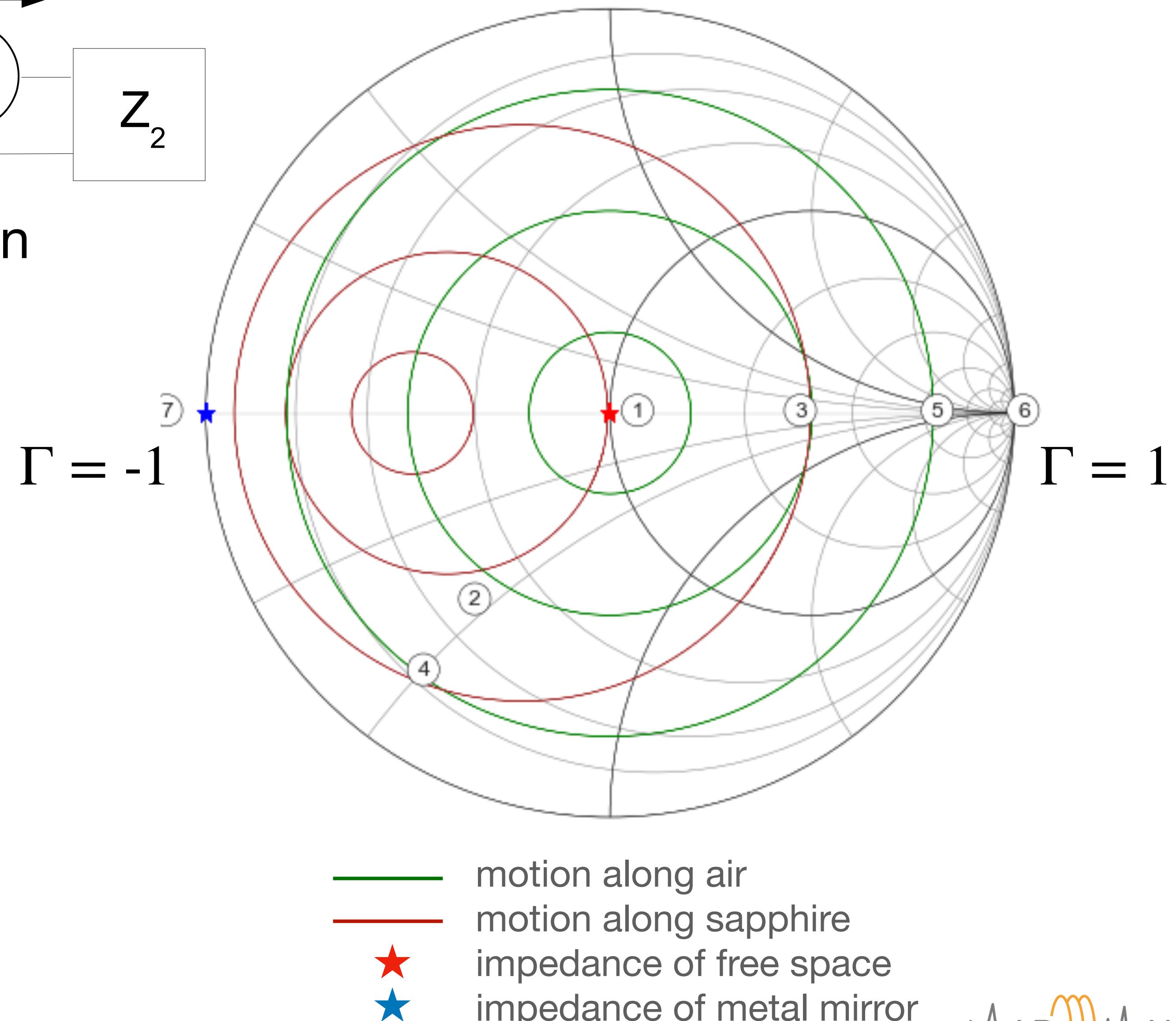
- Impedance transform:  $Z_0 \rightarrow 0$ .
- A special case of stepped-impedance filters, or generalized Bragg resonator



- Limitation: not considering emission from most disks, disk # < ~5

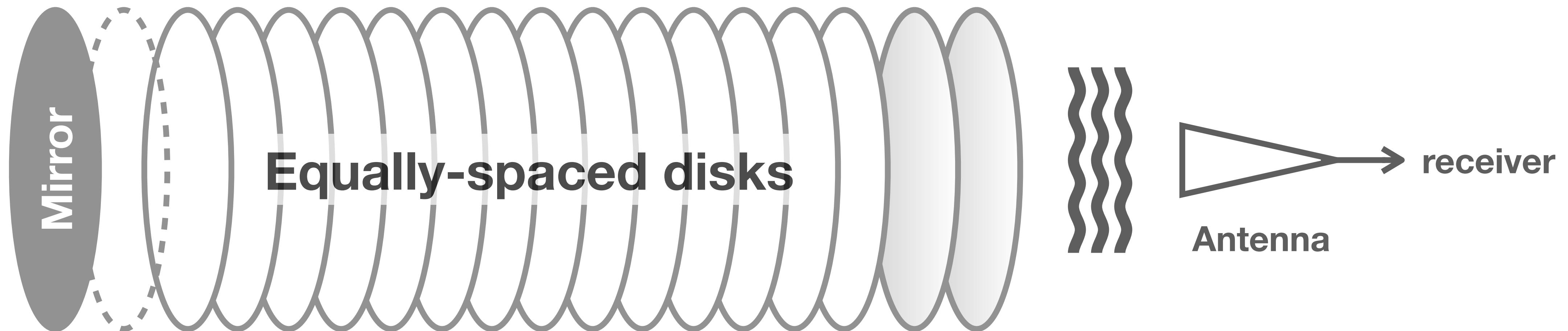


Normalized to  $Z_0 = 377\Omega$



# Disk spacing

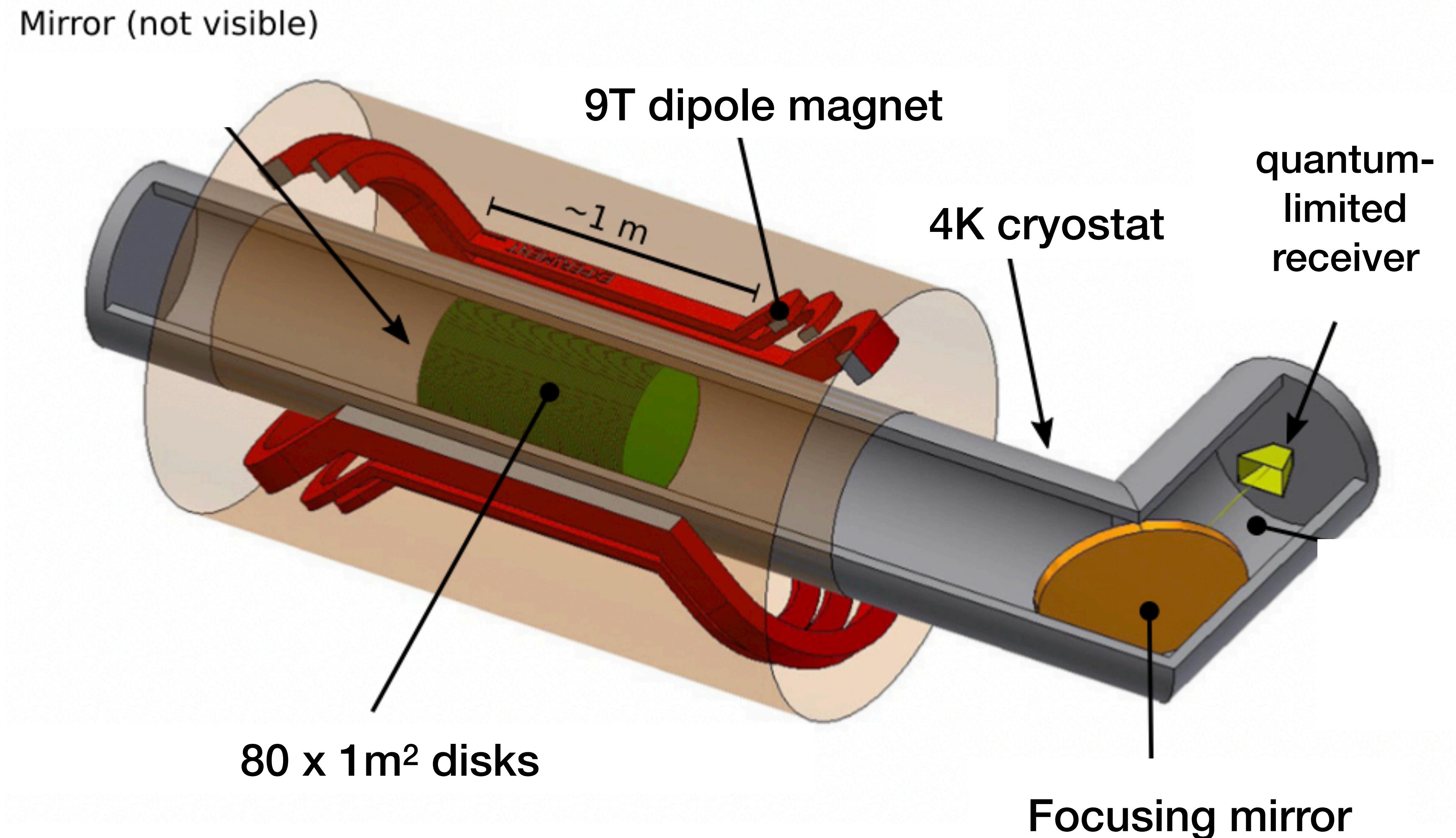
## “Waveguide structure”



	Mirror matching	equally-spaced disks	free space matching
<b>impedance</b>	0 to $Z_c$	characteristic impedance ( $Z_c$ )	$Z_c$ to $Z_0$
<b>air gap length</b>	$\sim \lambda/4^*$	from <b>Bloch impedance</b>	impedance transform
<b># of disks</b>	0~1	>2	1~2

# Ultimate dielectric haloscope

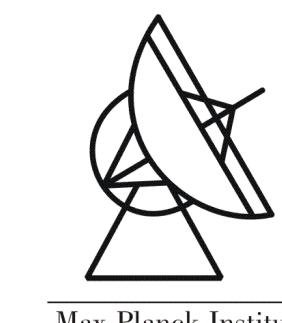
## Sensitive to post-inflationary QCD-axion



# MADMAX collaboration



Axions beyond Gen 2, Univ. of Washington, Jan 2021



NÉEL  
institut

Max-Planck-Institut  
für Radioastronomie



CENTRE DE PHYSIQUE DES  
PARTICULES DE MARSEILLE  
CPPM

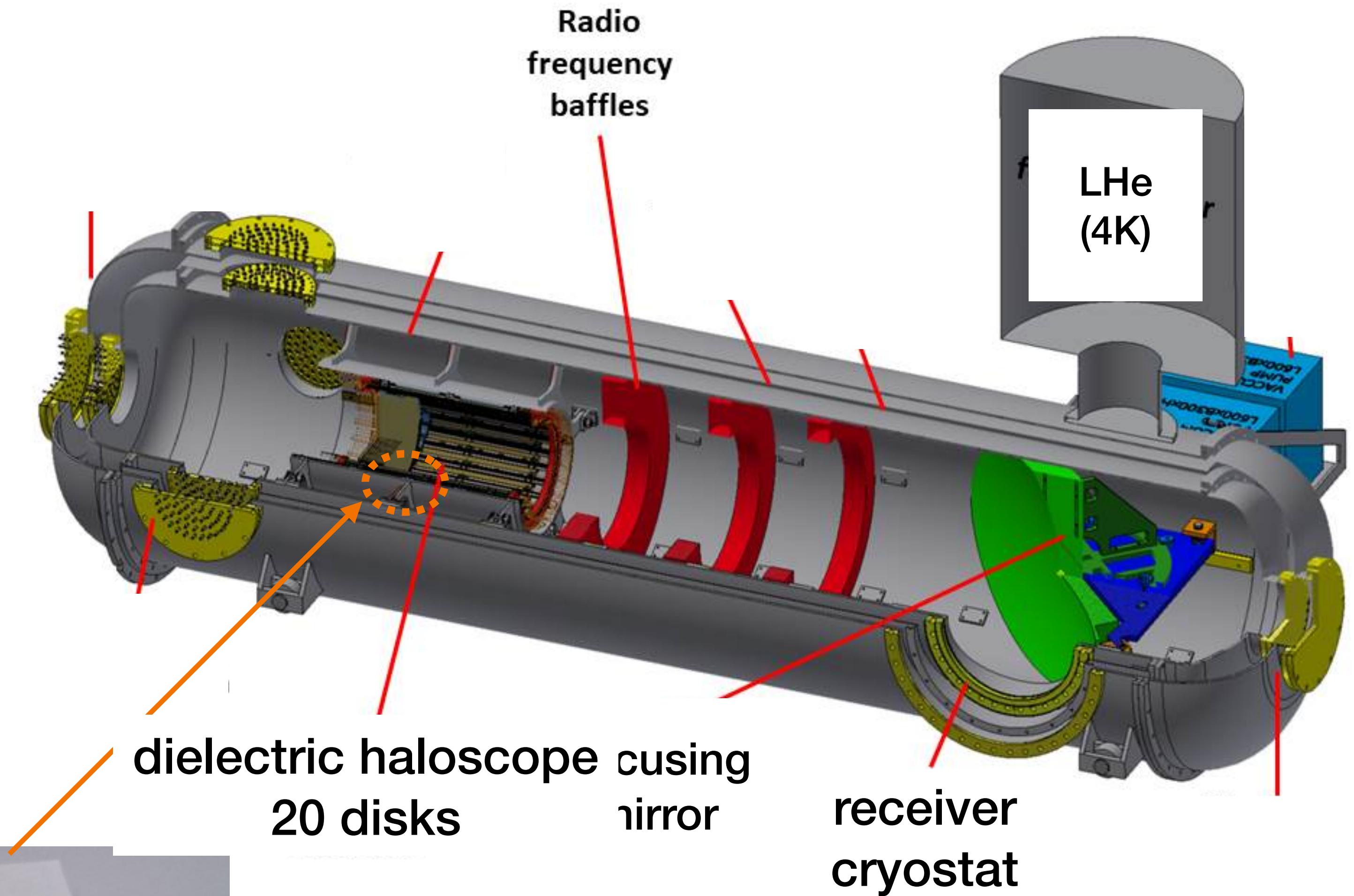
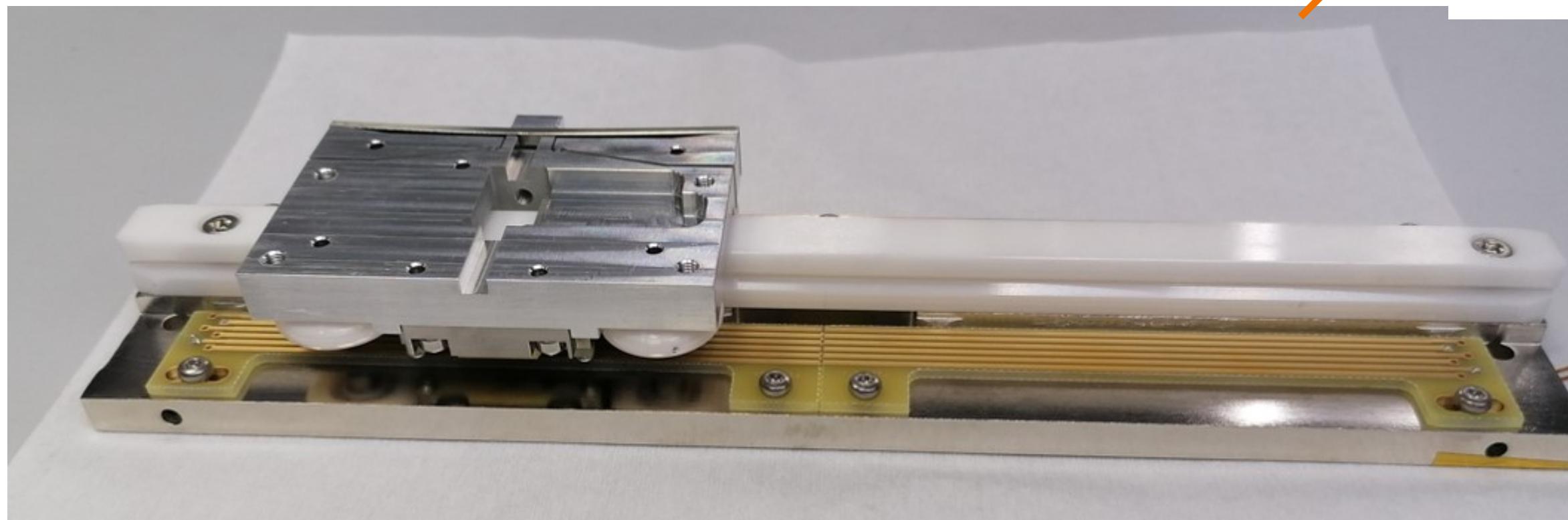


Universidad  
Zaragoza



# Prototype

- R&D platform
- Cryostat design fixed
- ALPs / HP search



Cryogenic piezo positioner & laser interferometer assembly

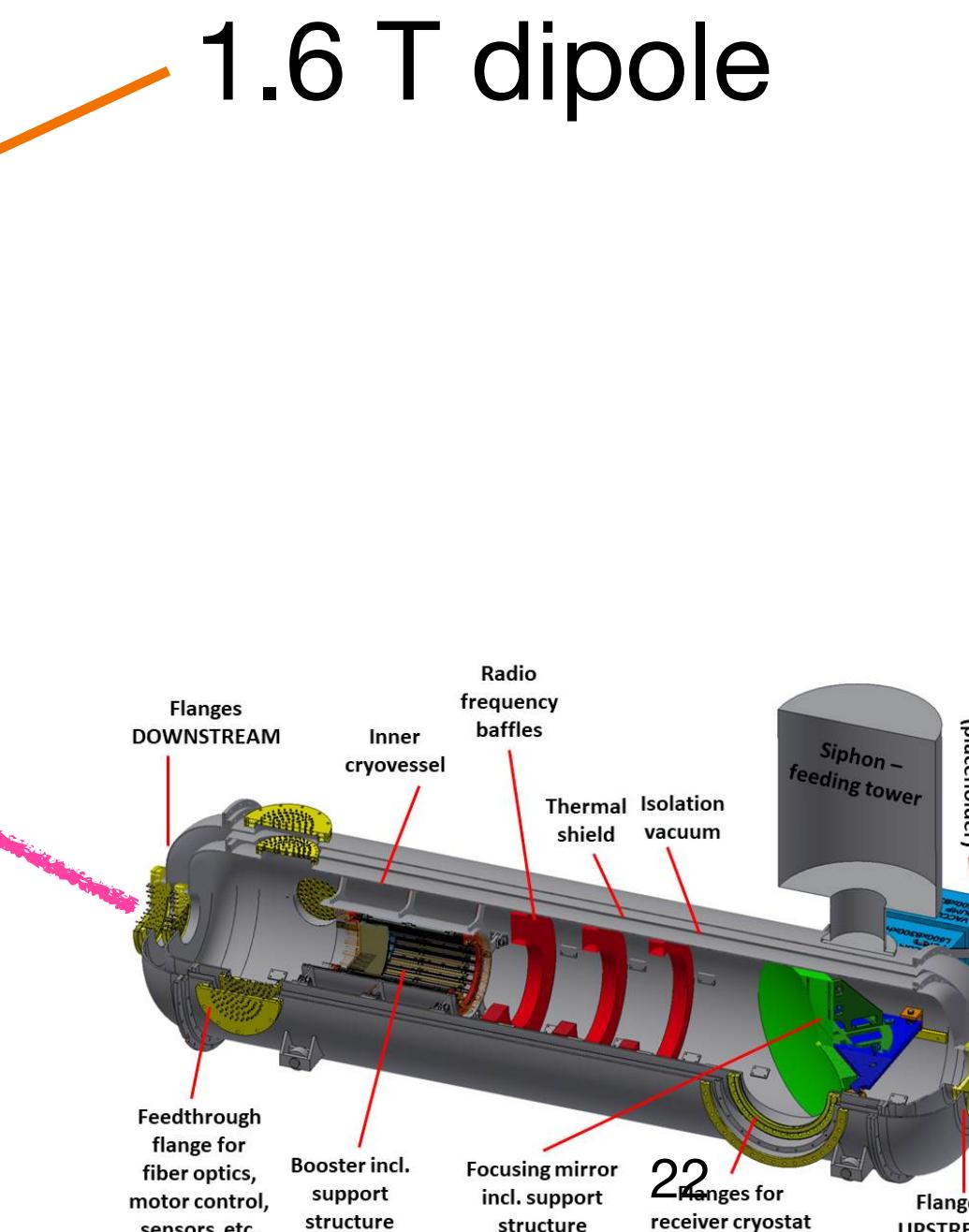
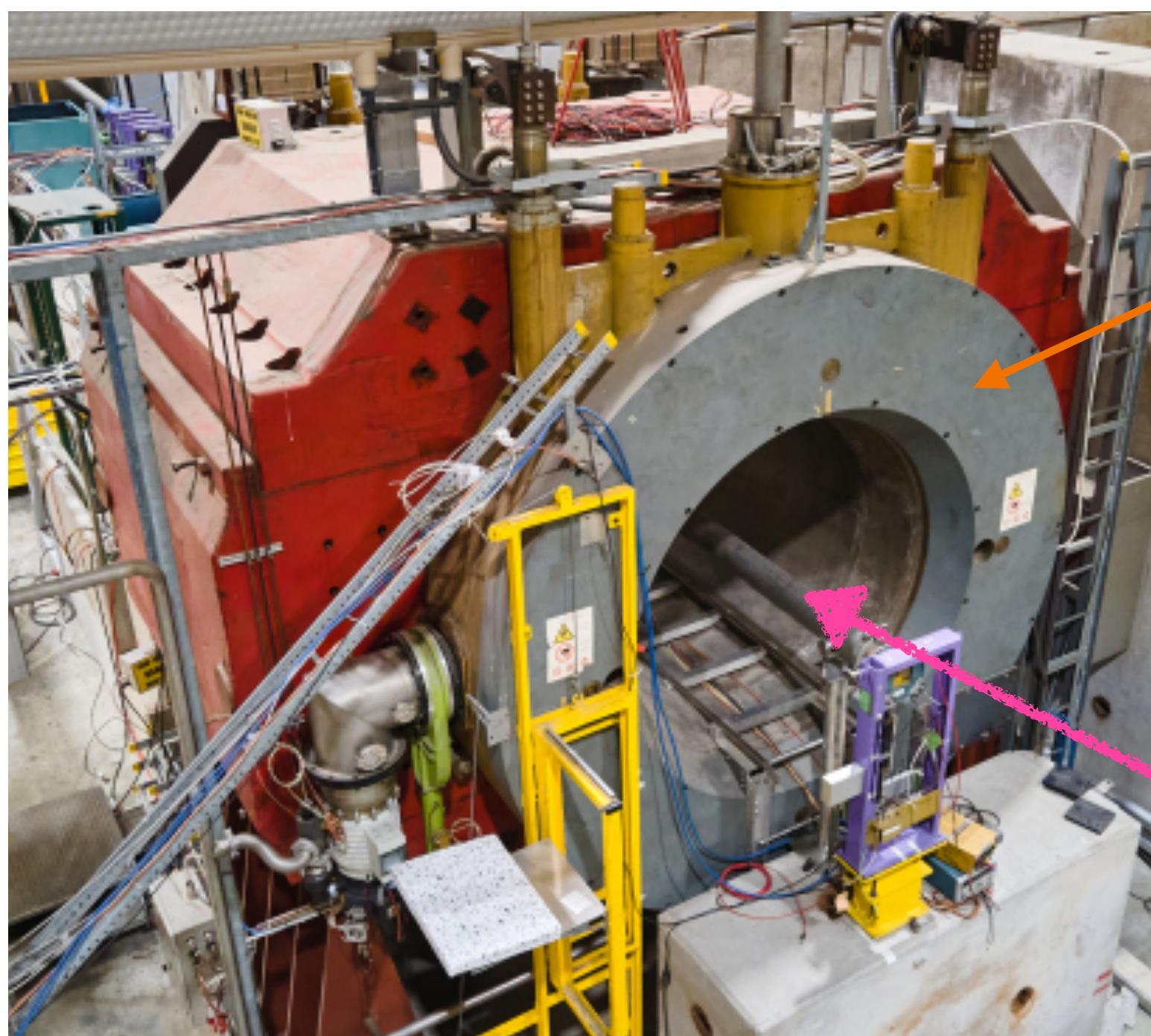
# MADMAX and CERN's Morpurgo magnet

A new collaboration, MADMAX, will seize the chance to use a CERN magnet named Morpurgo to test their dark-matter prototype

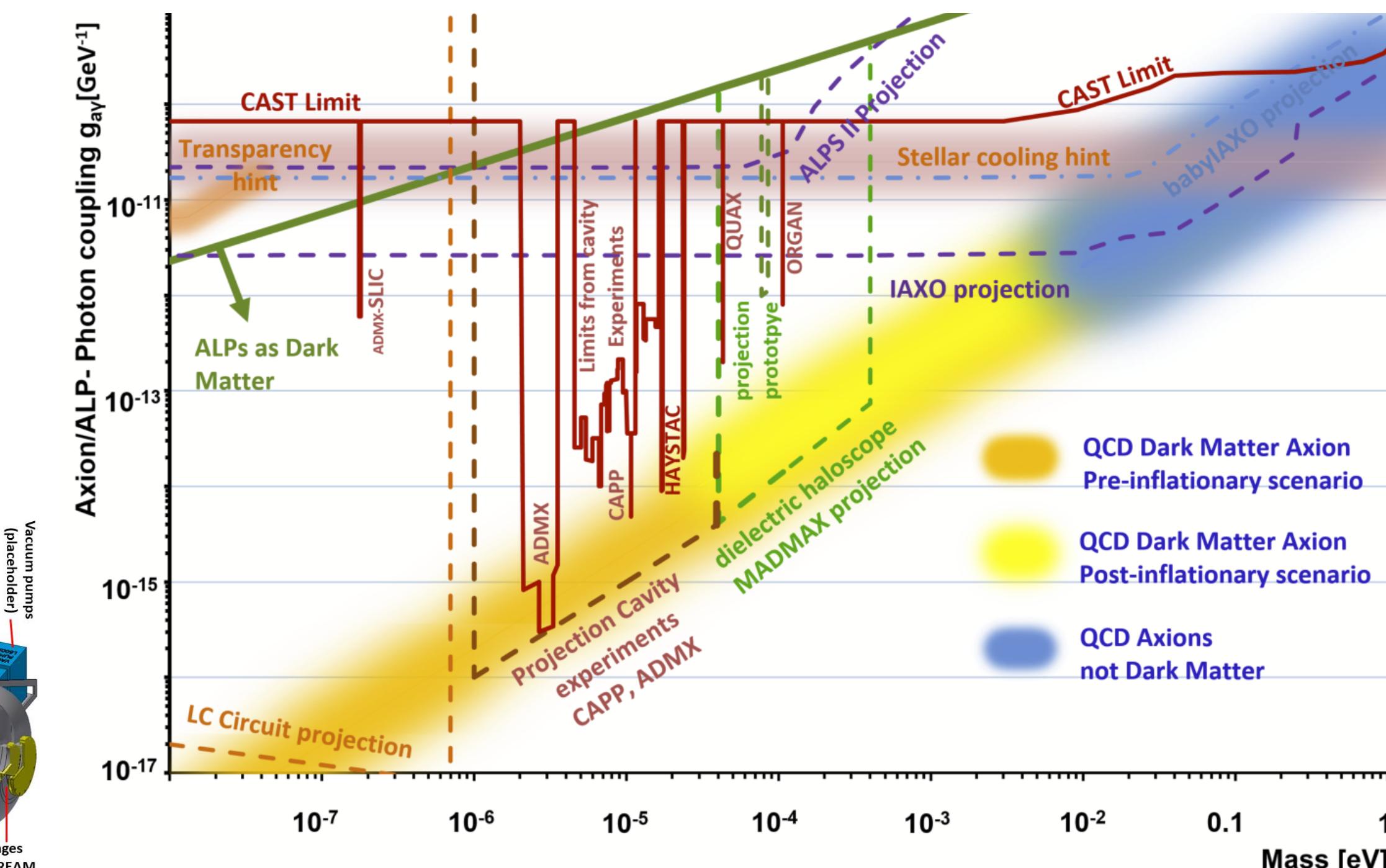
CERN Bulletin

<https://home.cern/news/news/experiments/madmax-and-cerns-morpurgo-magnet>

10 NOVEMBER, 2020 | By Thomas Hortala



- Test of the components in B-field during the SPSS shut down

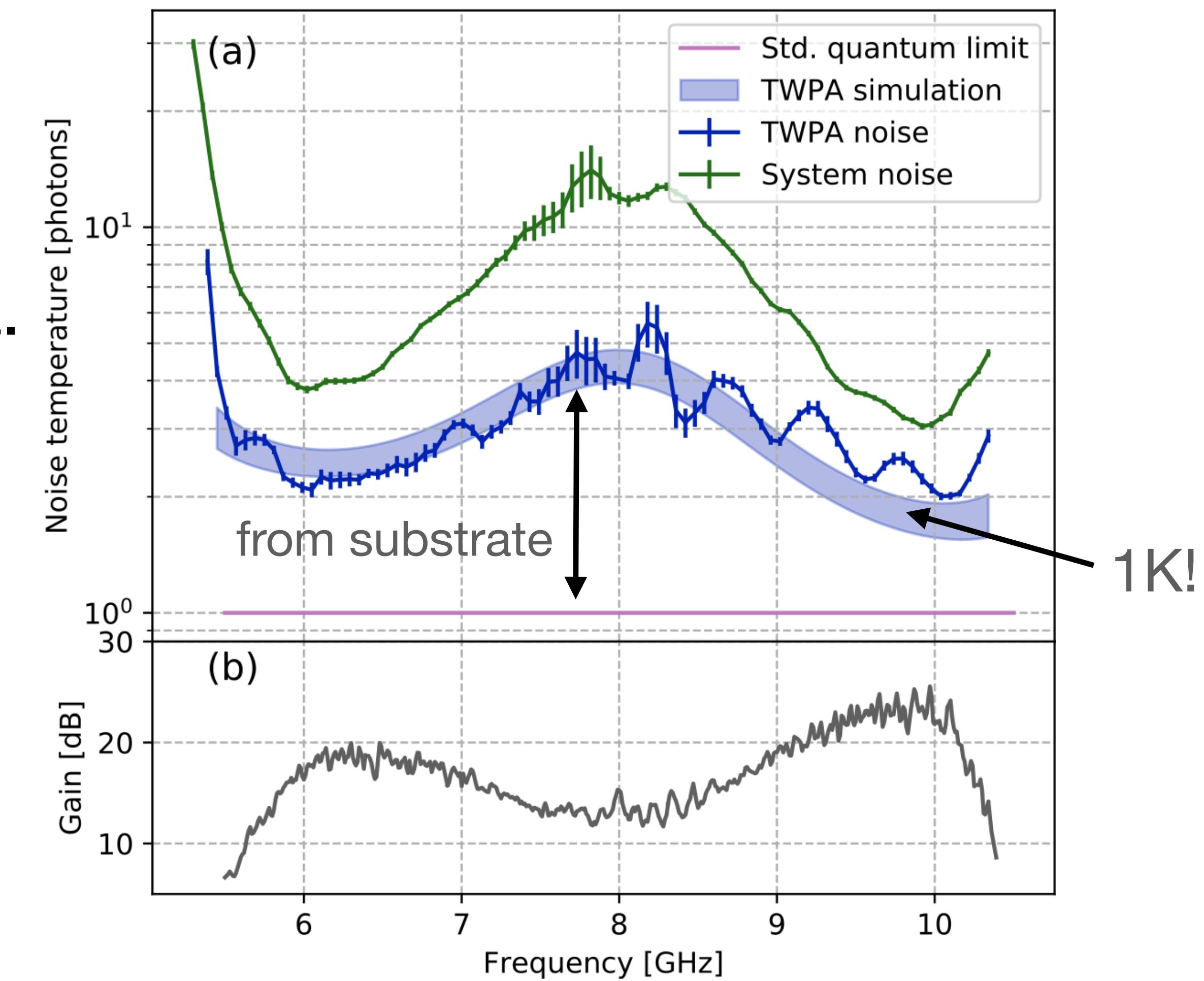
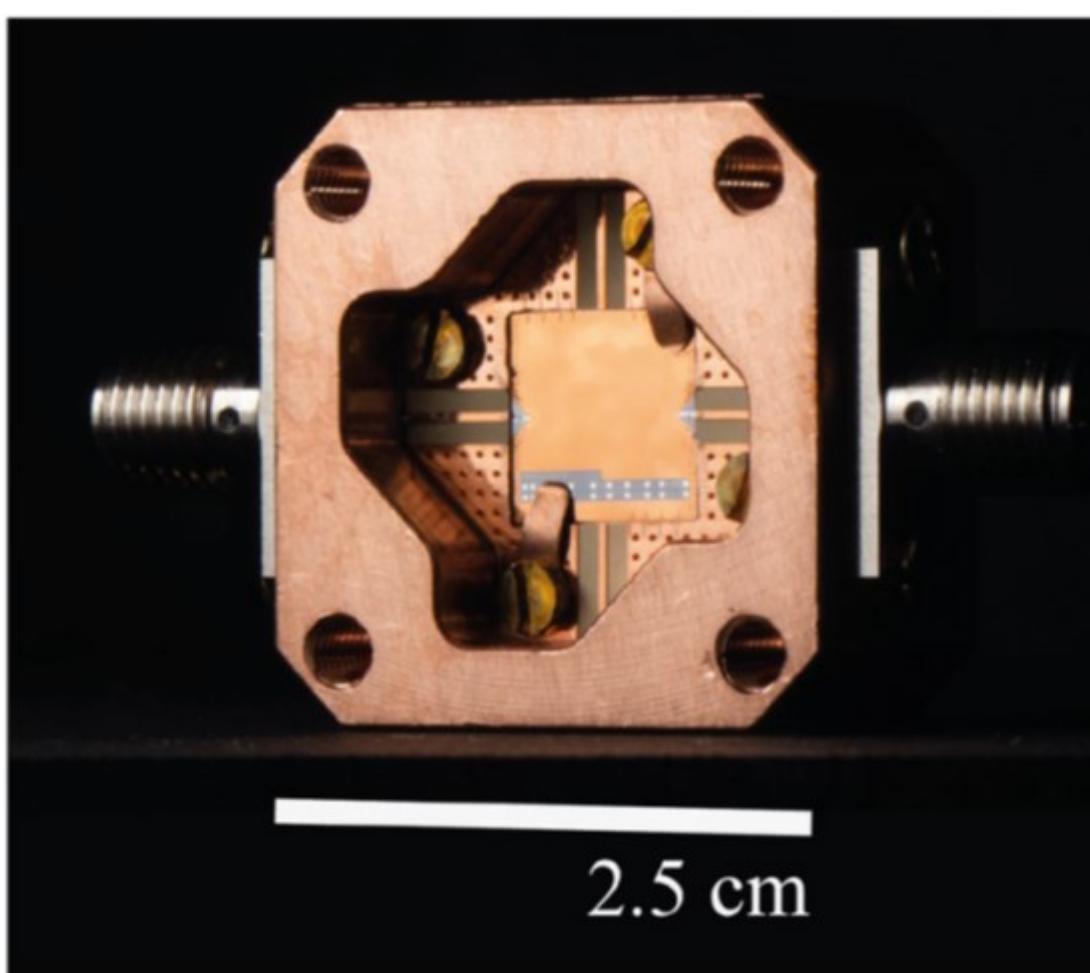


# Quantum-limited amplifier

## Traveling wave parametric amplifier (TWPA)



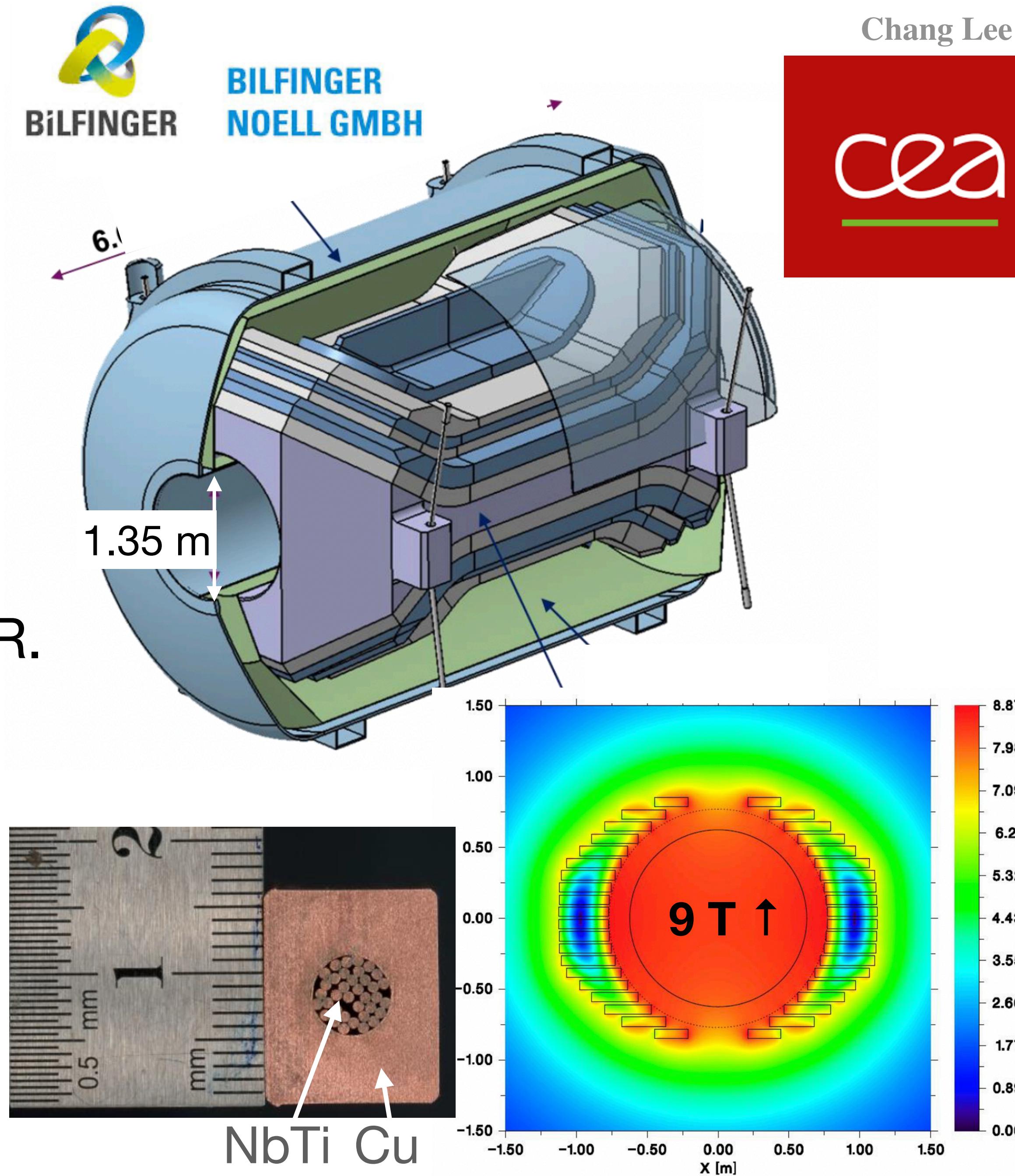
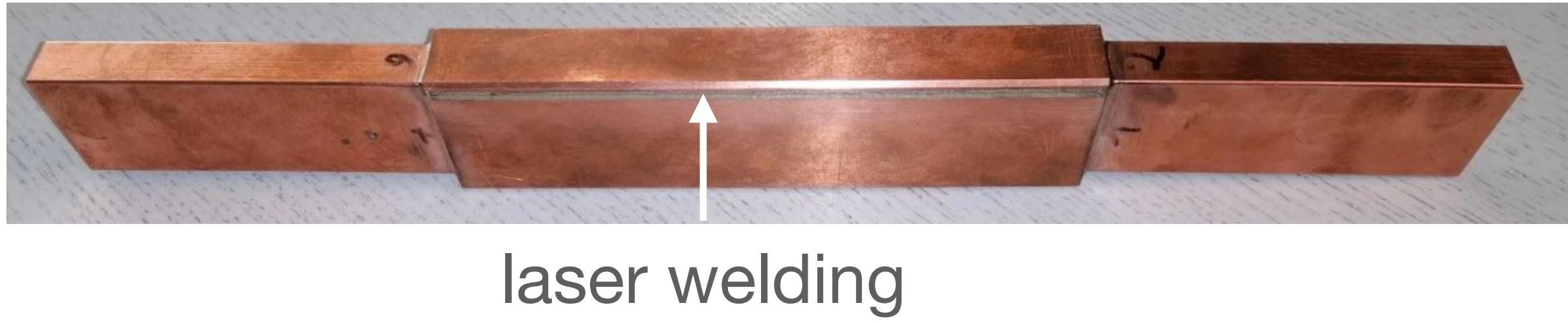
- **First 10 GHz TWPA produced.**  
PRX 10, 021021
- 1K noise temp, 20 dB gain @ 10 GHz.
- Future development to 30 GHz.



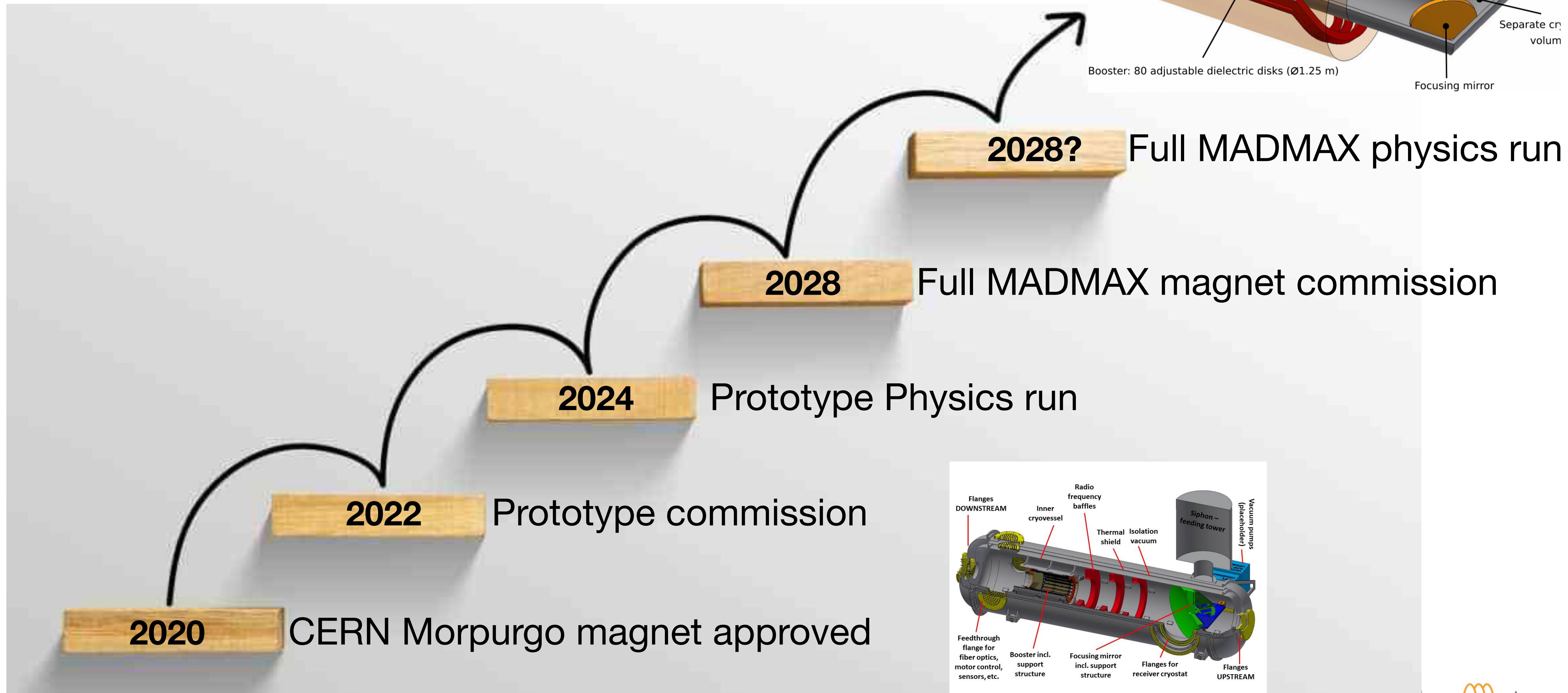
# Magnet development

## Full scale MADMAX magnet

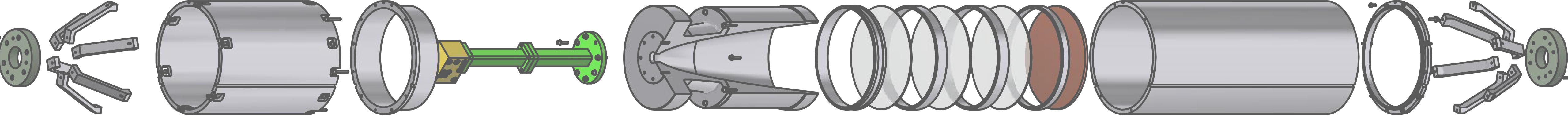
- 9T, 1.35-m warm bore **dipole** magnet
- Superconducting CICC w/ Cu jacket
  - experience and infrastructure from ITER.
- Quench test: 1/2 size mockup coil



# Timeline



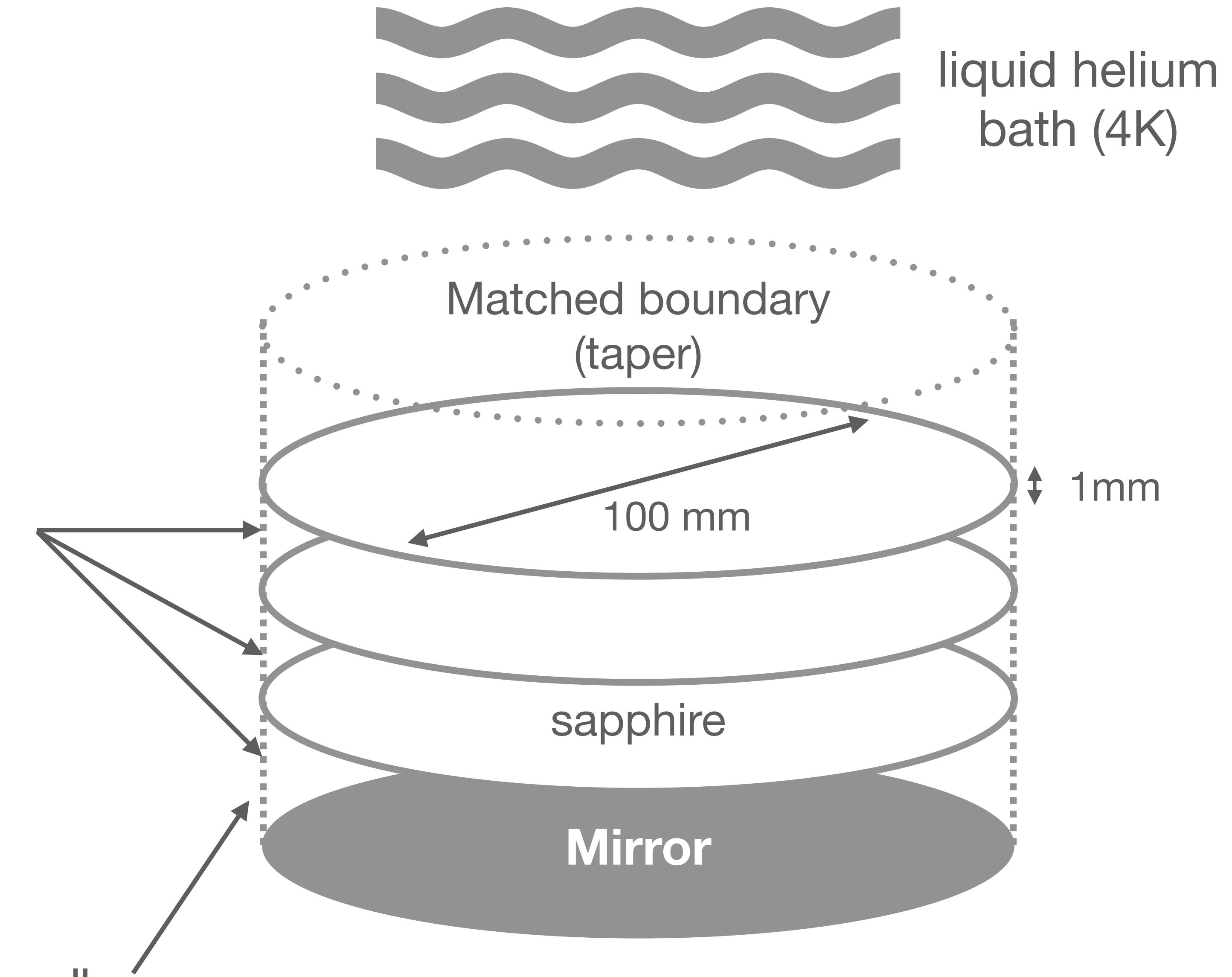
# 100mm LHe setup



# Overview

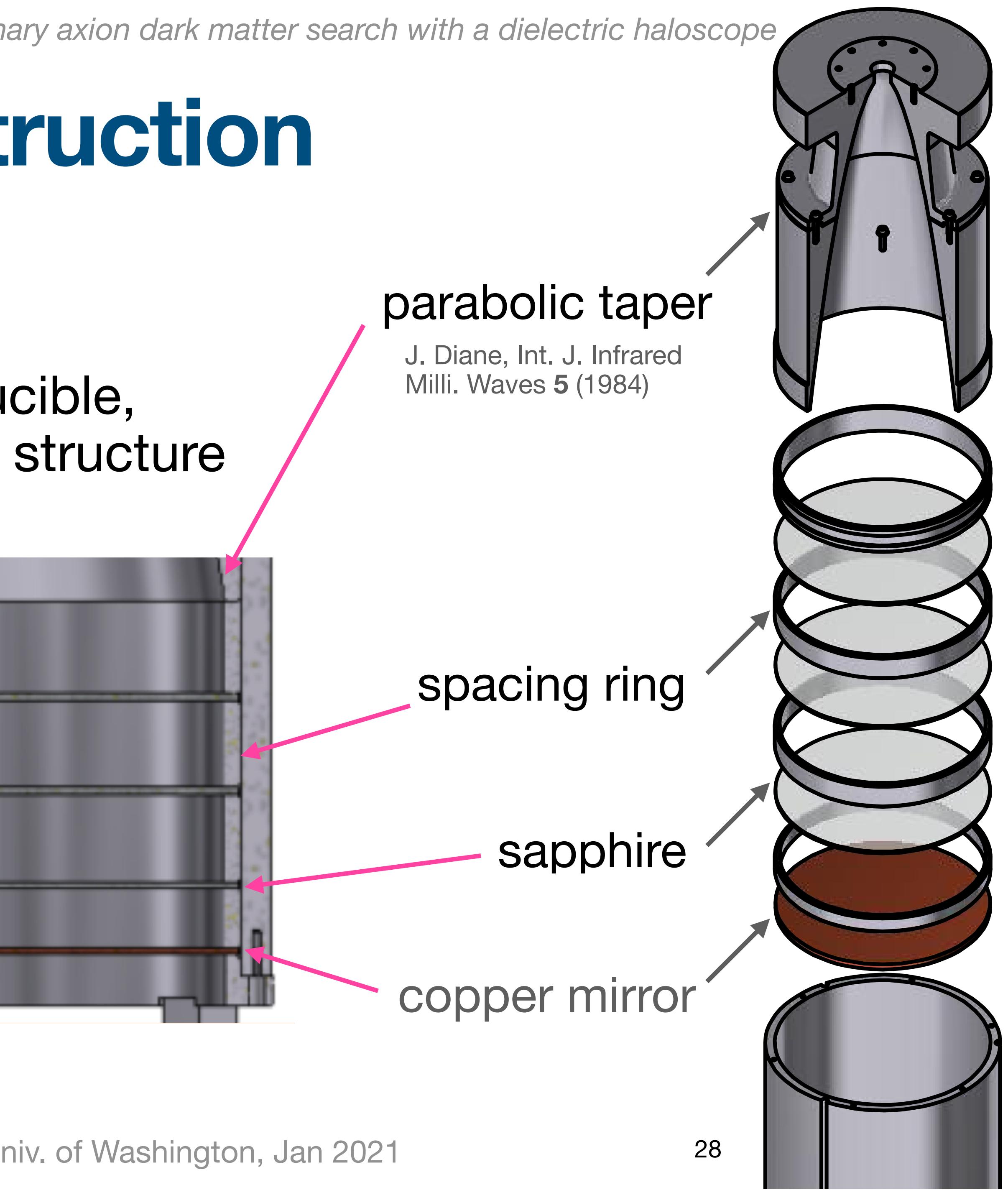
- Proof-of-principle
- Resonance @ 19 GHz
  - Air gaps from impedance matching
- Closed system w/ taper

closed system: metallic walls



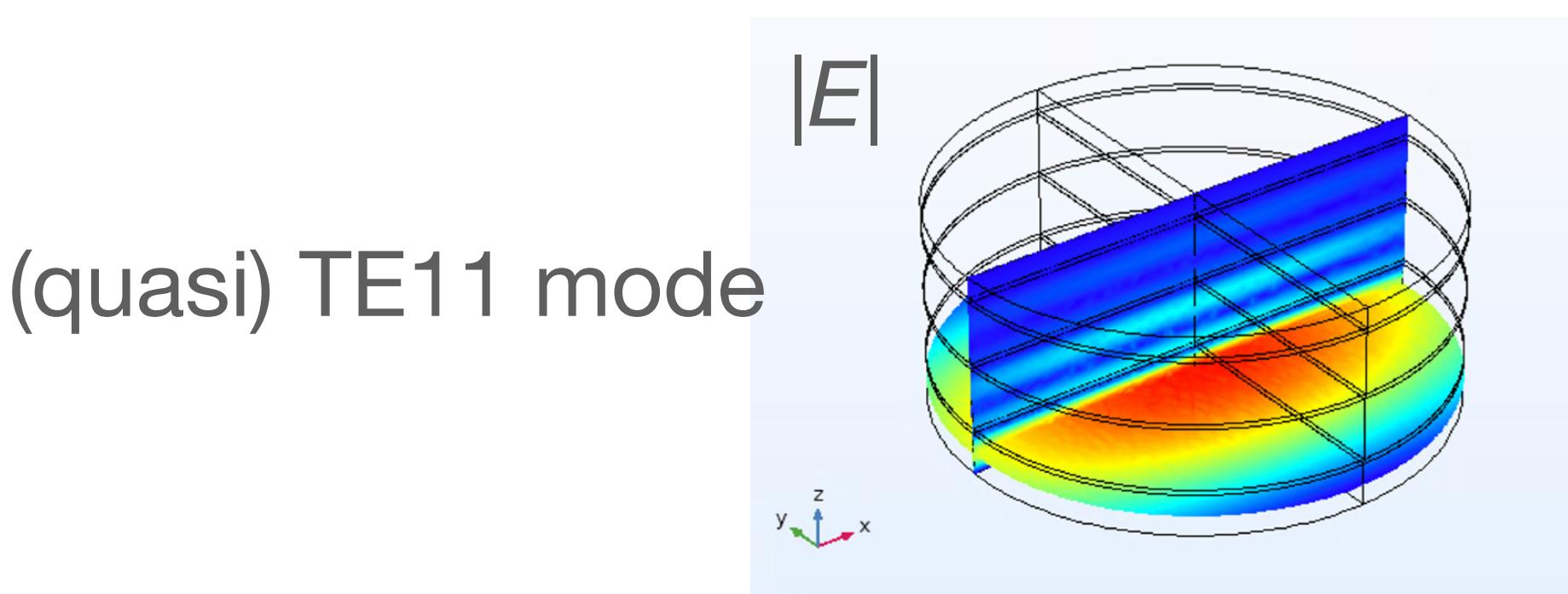
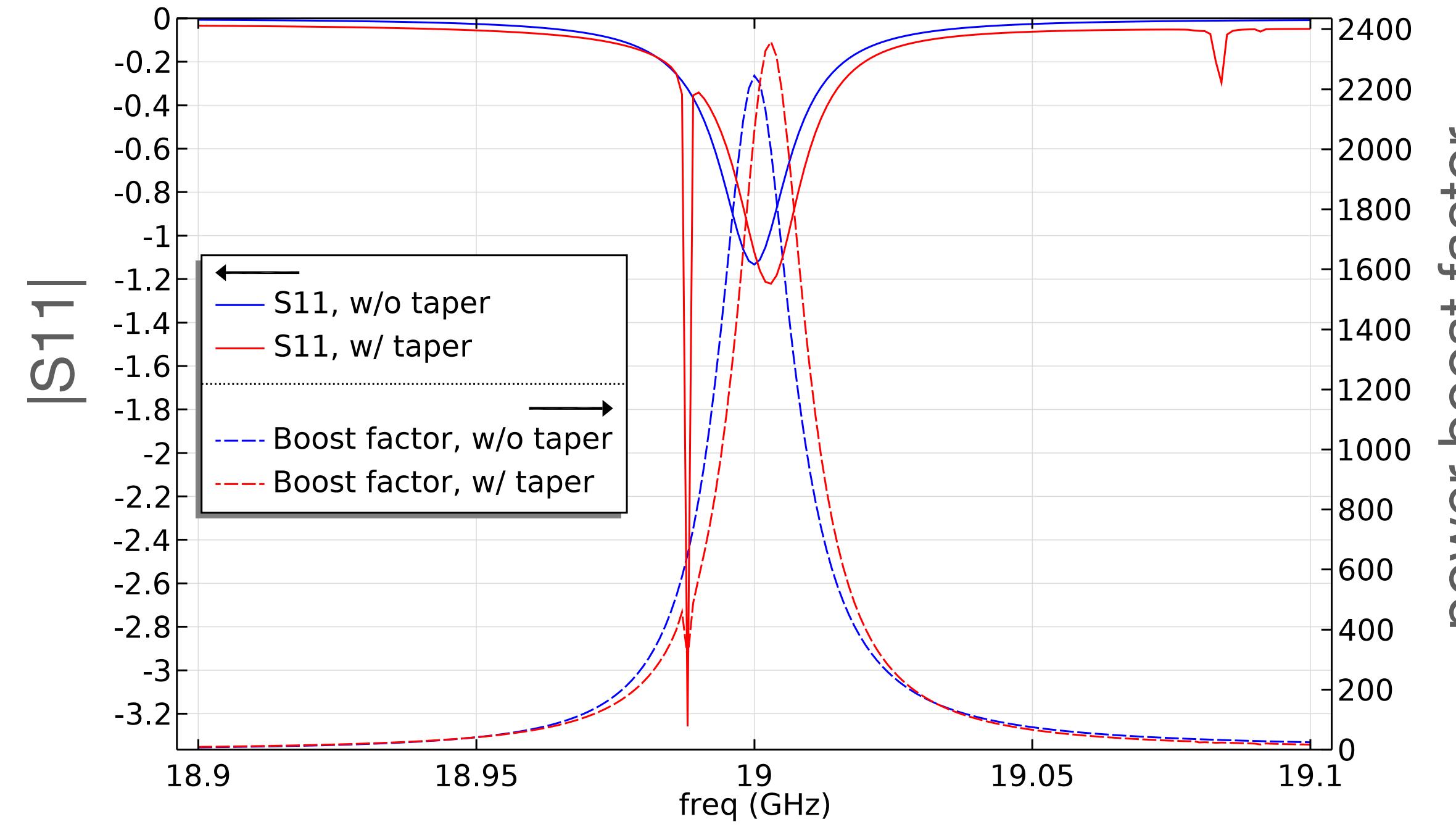
# Construction

- Reproducible, modular structure

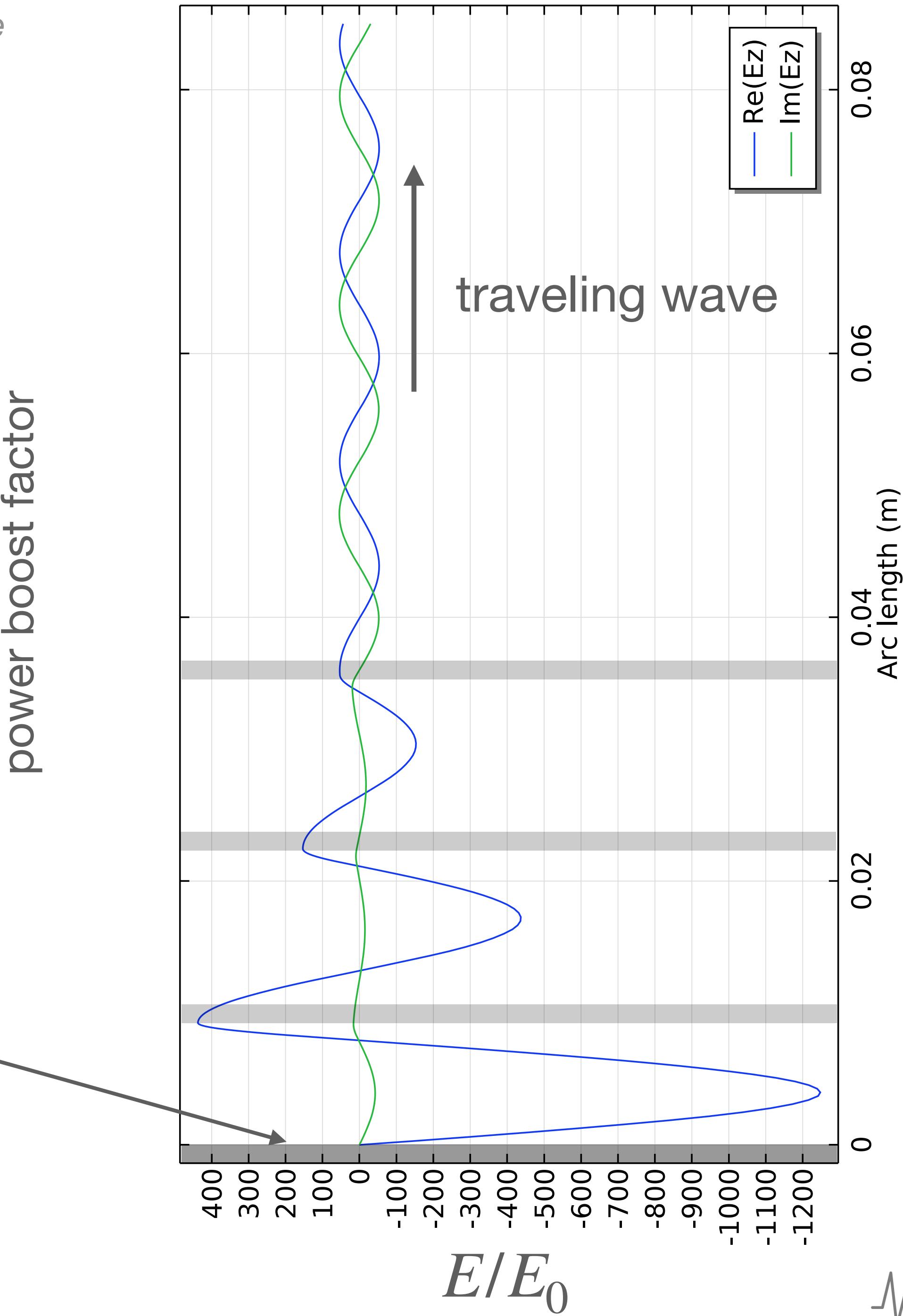


# Simulation

## Dielectric haloscope EM response



Major loss  
@ Cu mirror



parabolic  
taper

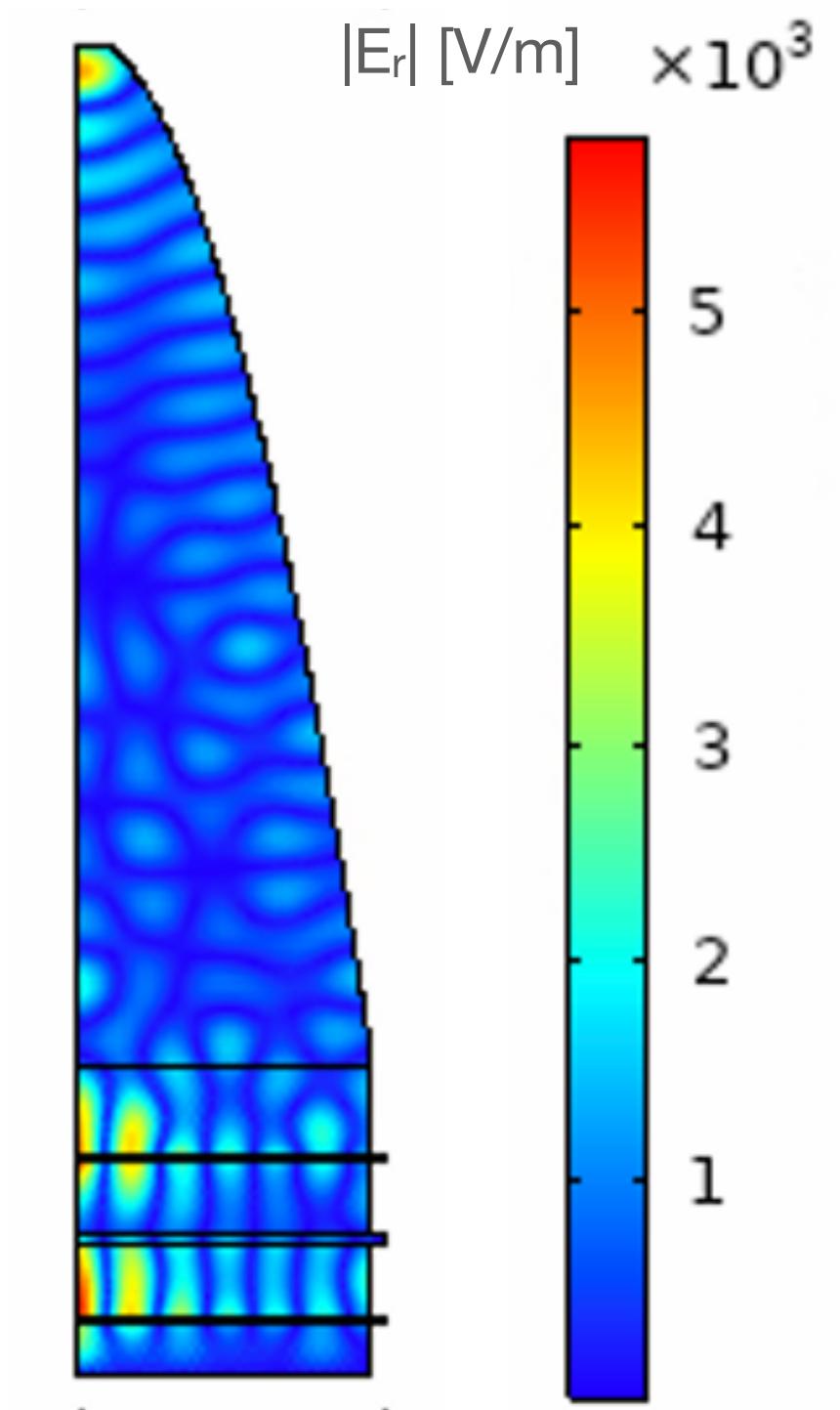
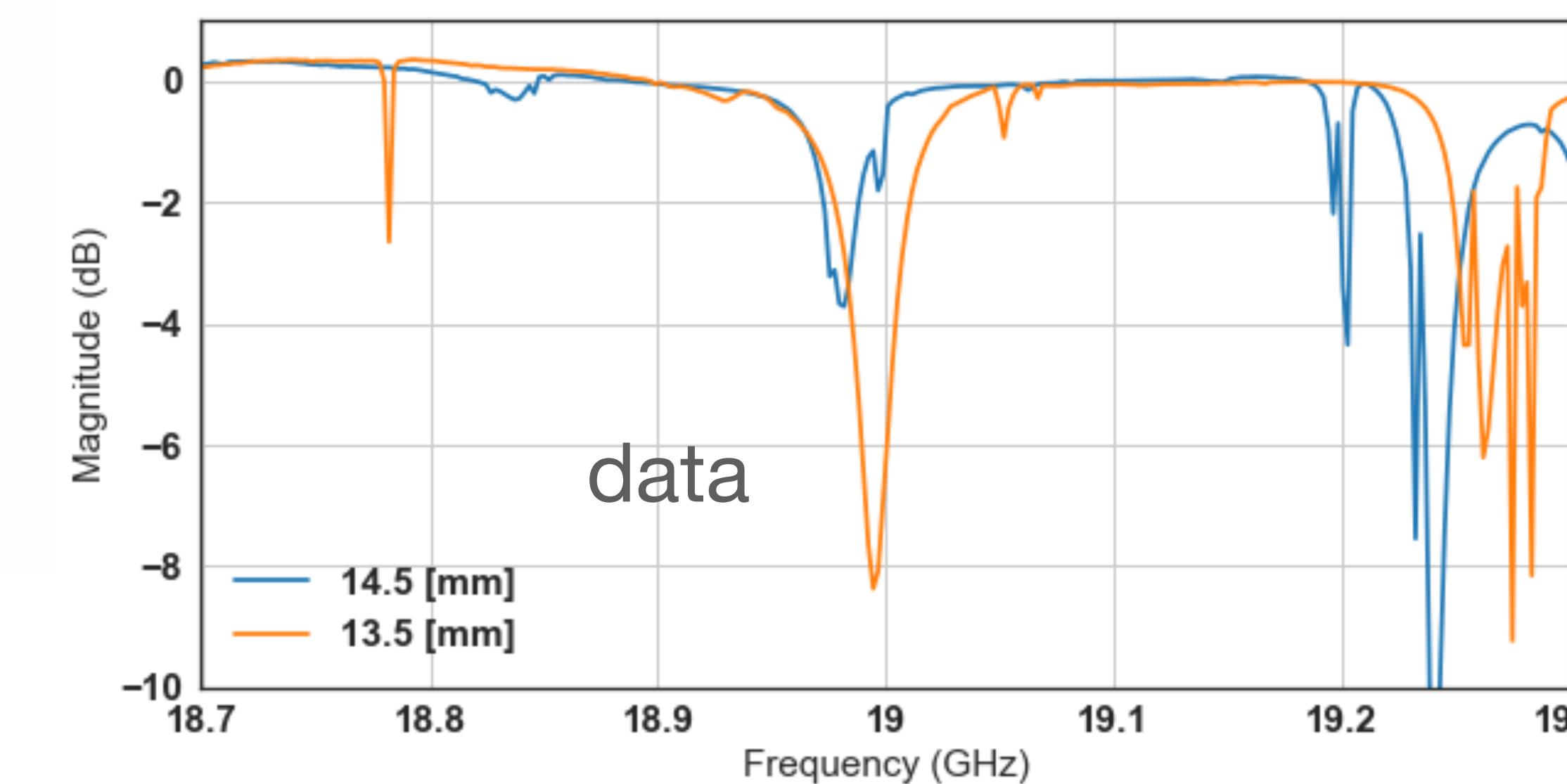
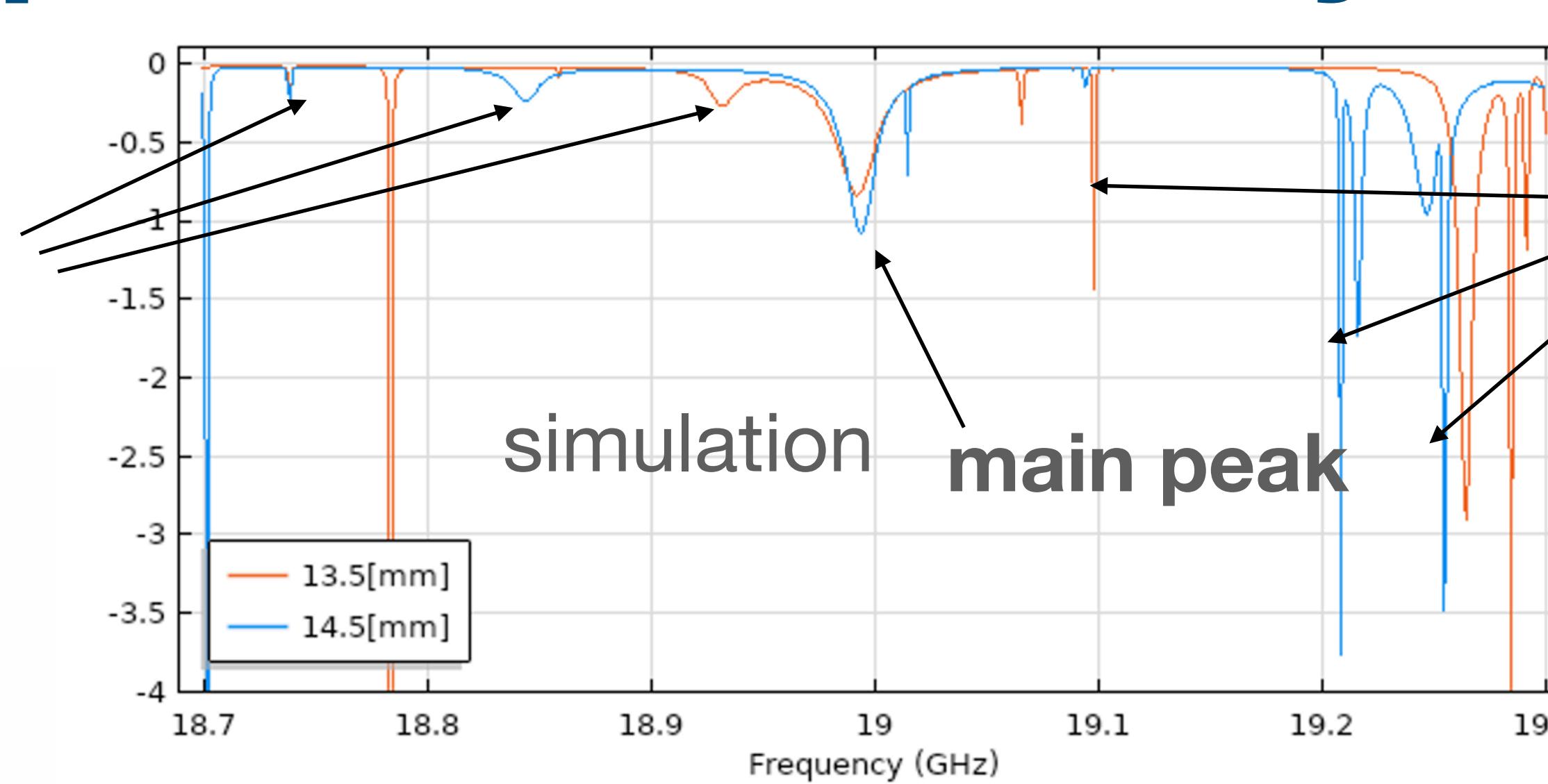
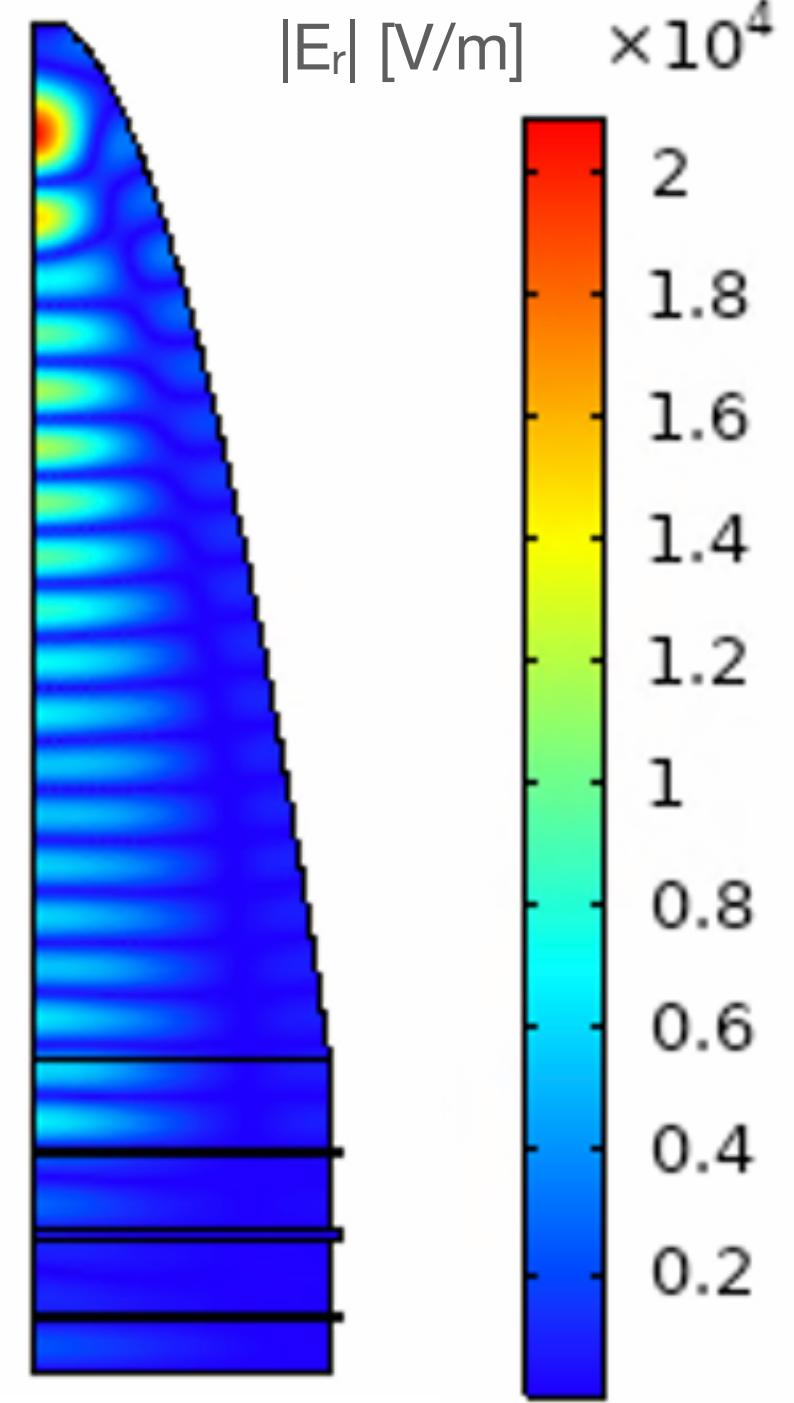
circular-  
rectangular  
WG  
transition



# Room temperature reflectivity

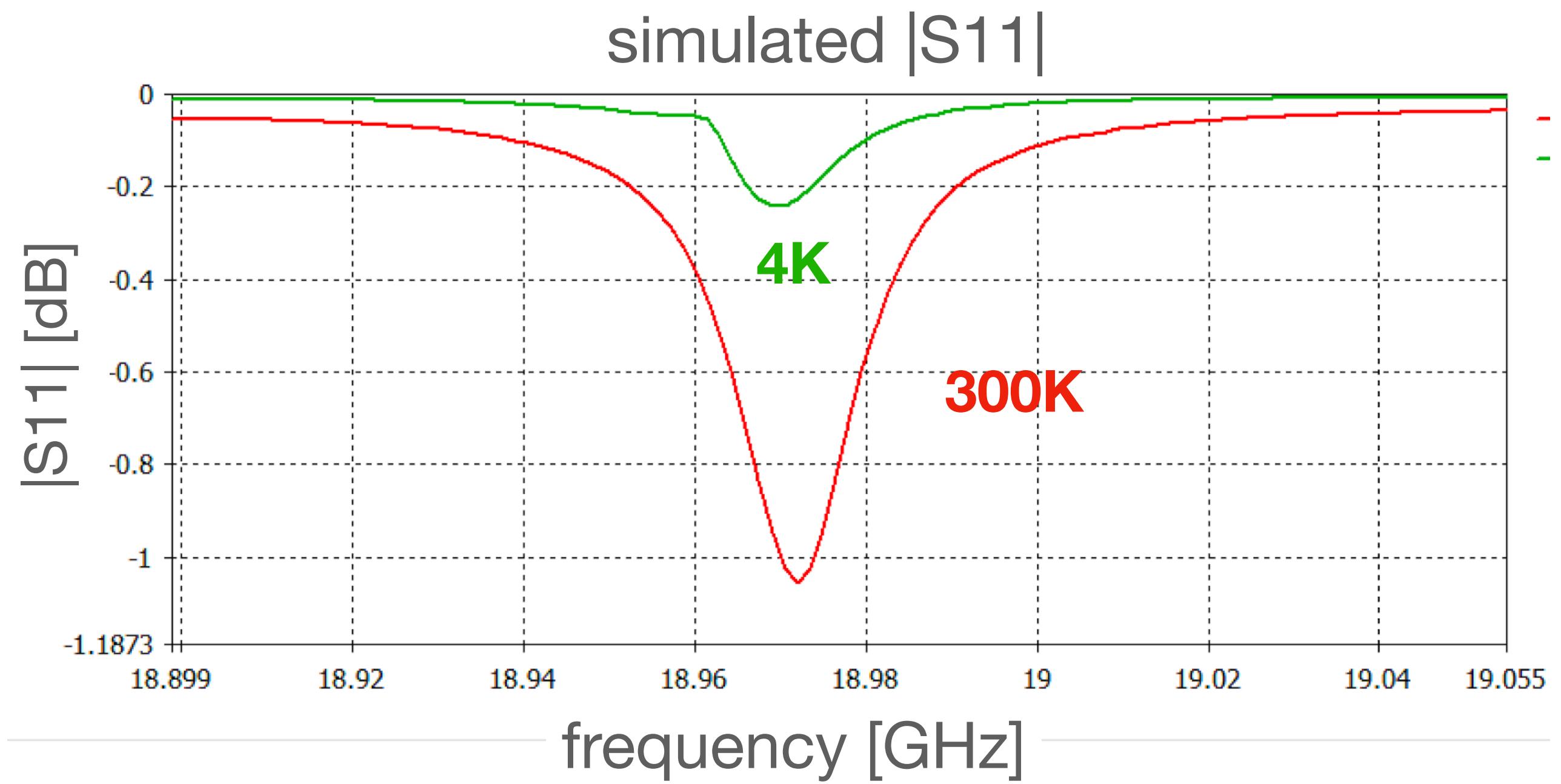
COMSOL simulation by X. Li

Taper modes



# Cryogenic operation

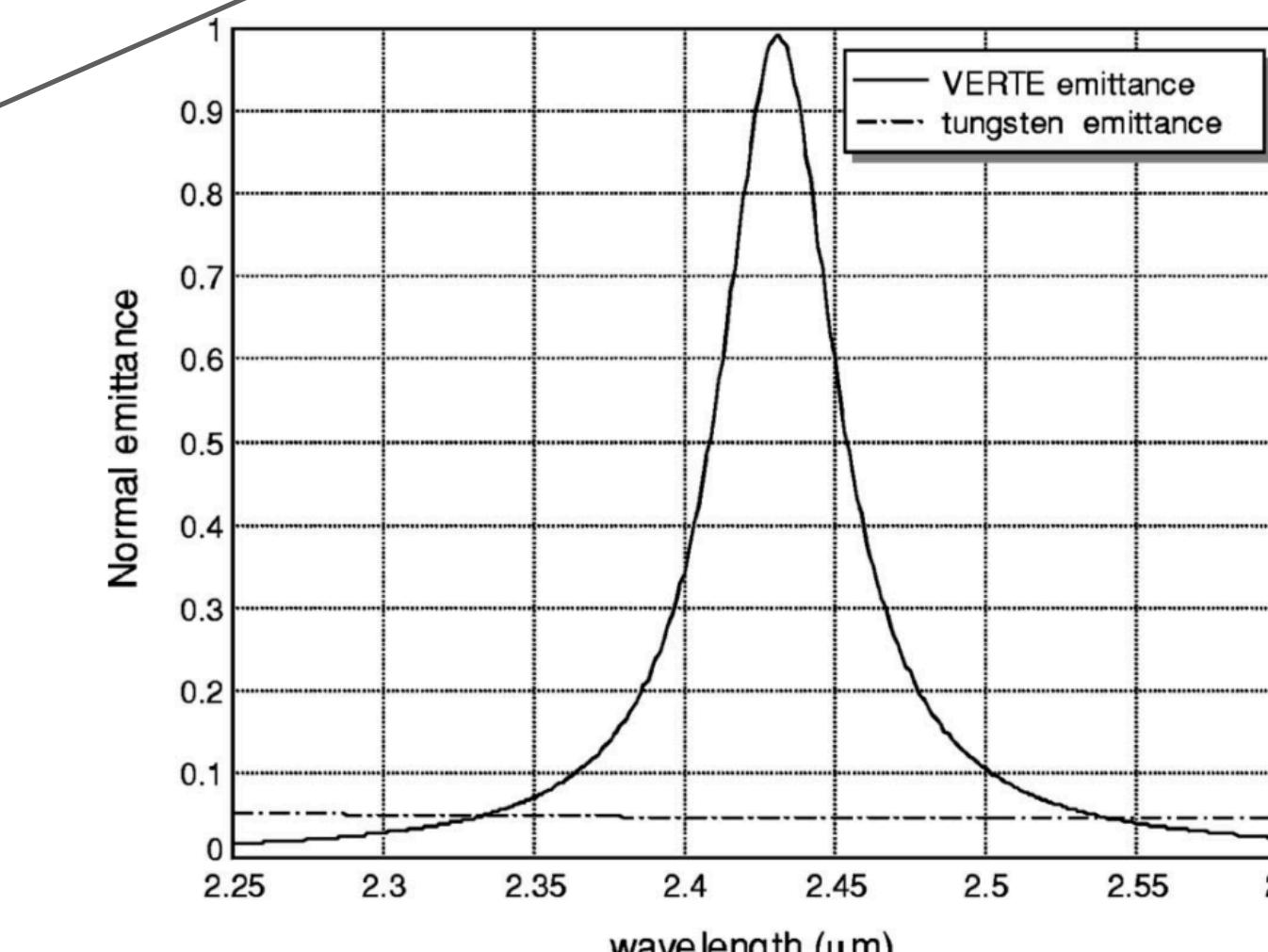
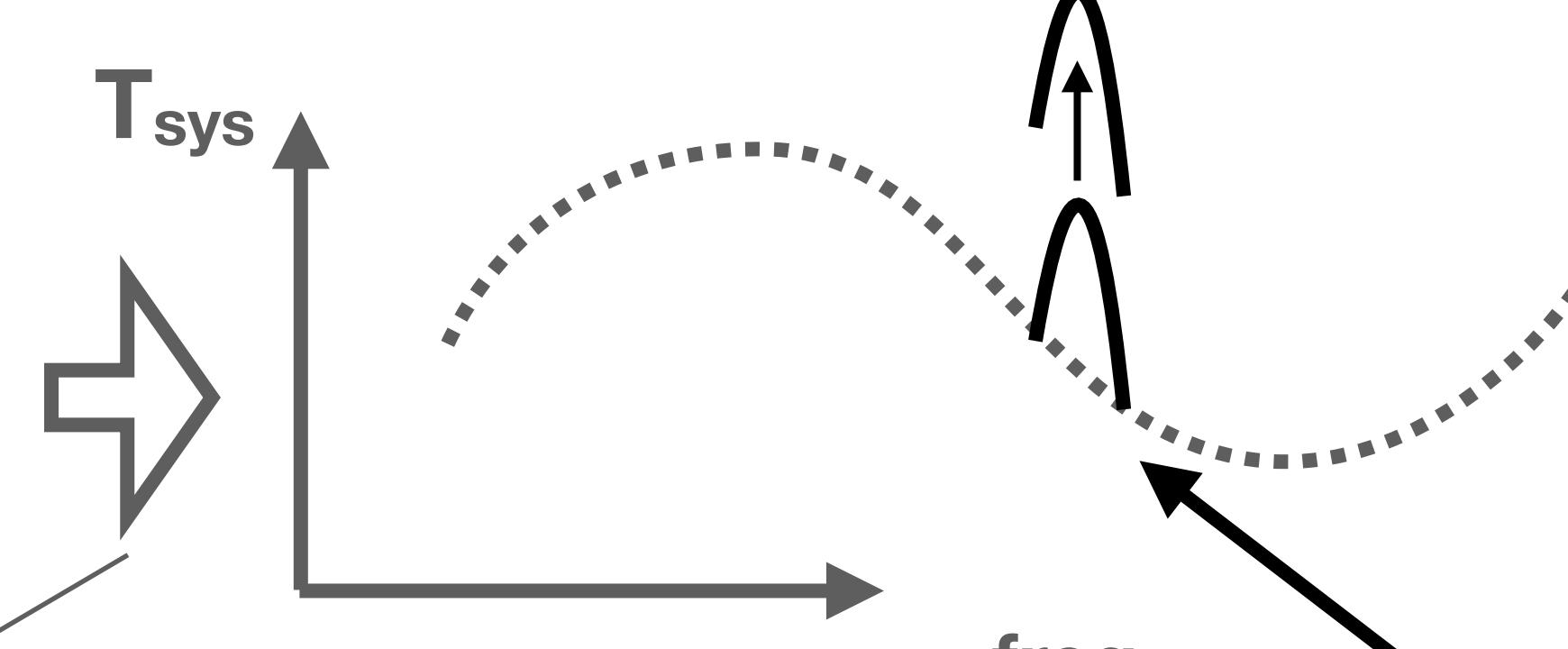
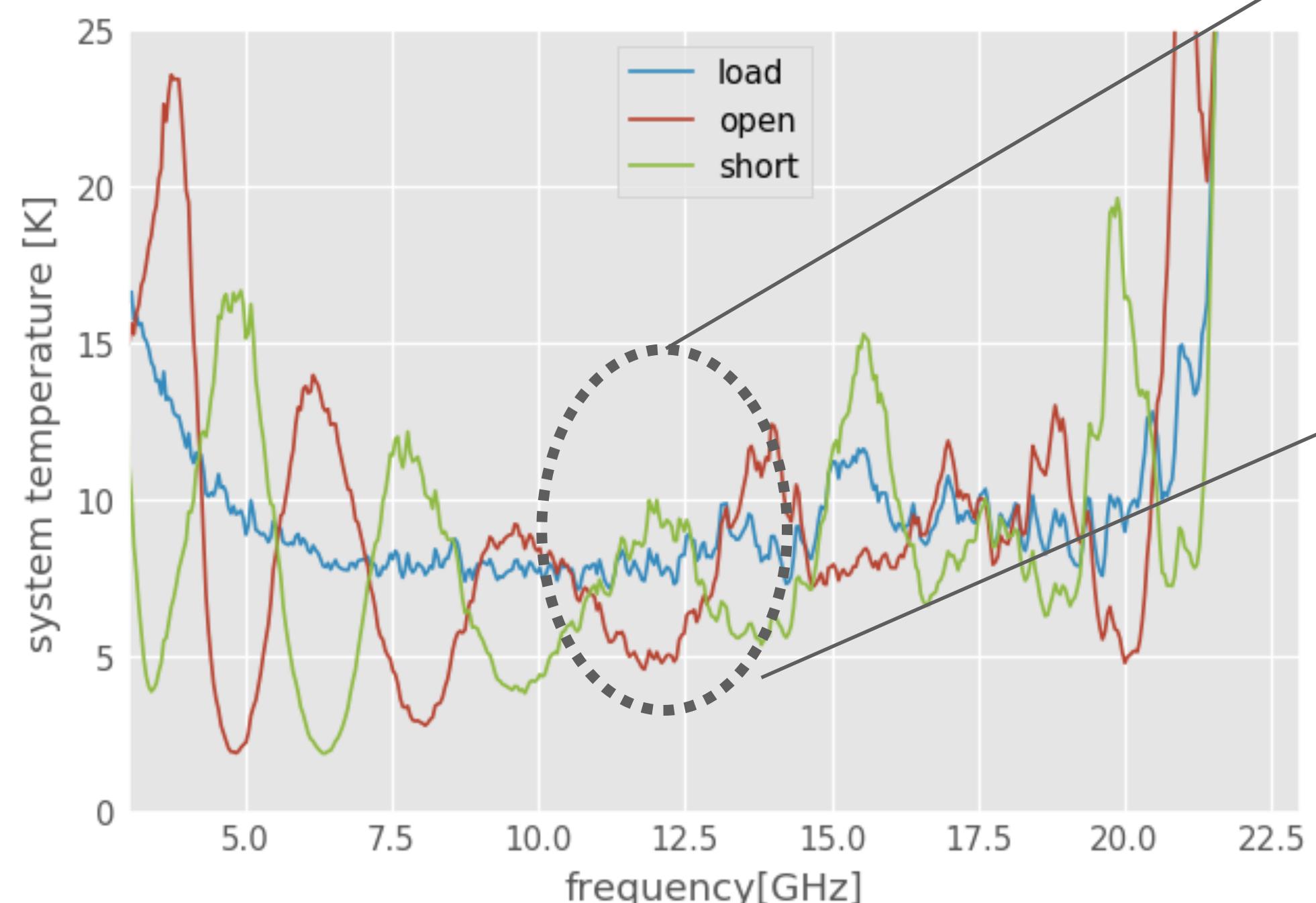
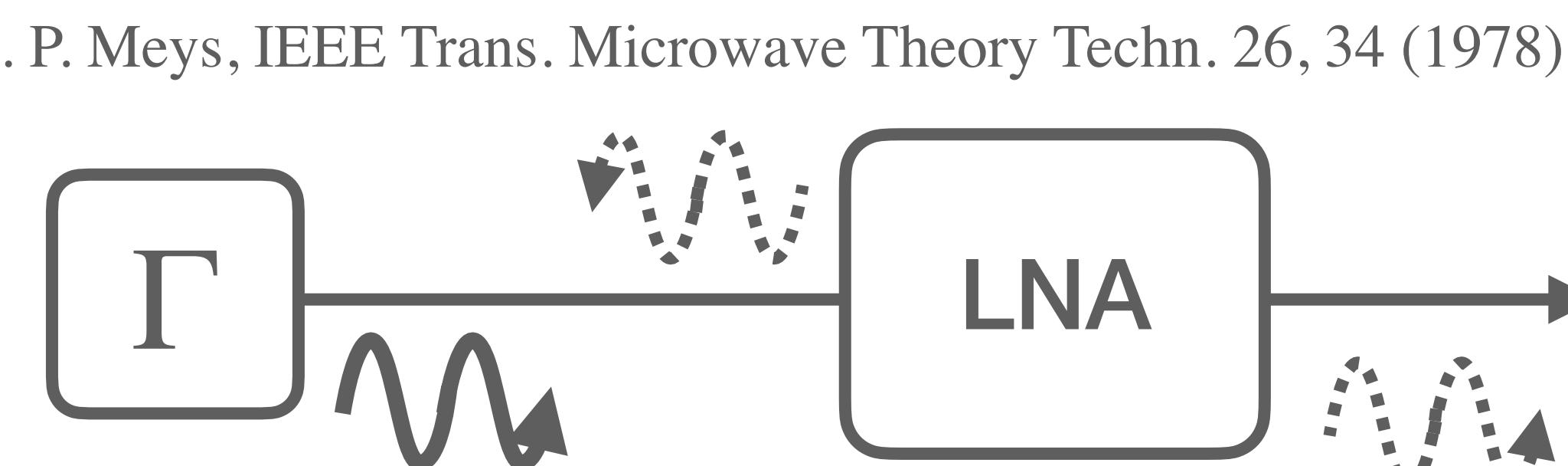
- Cryostat is ready.
- RF calibrated down to circular WG at 4K



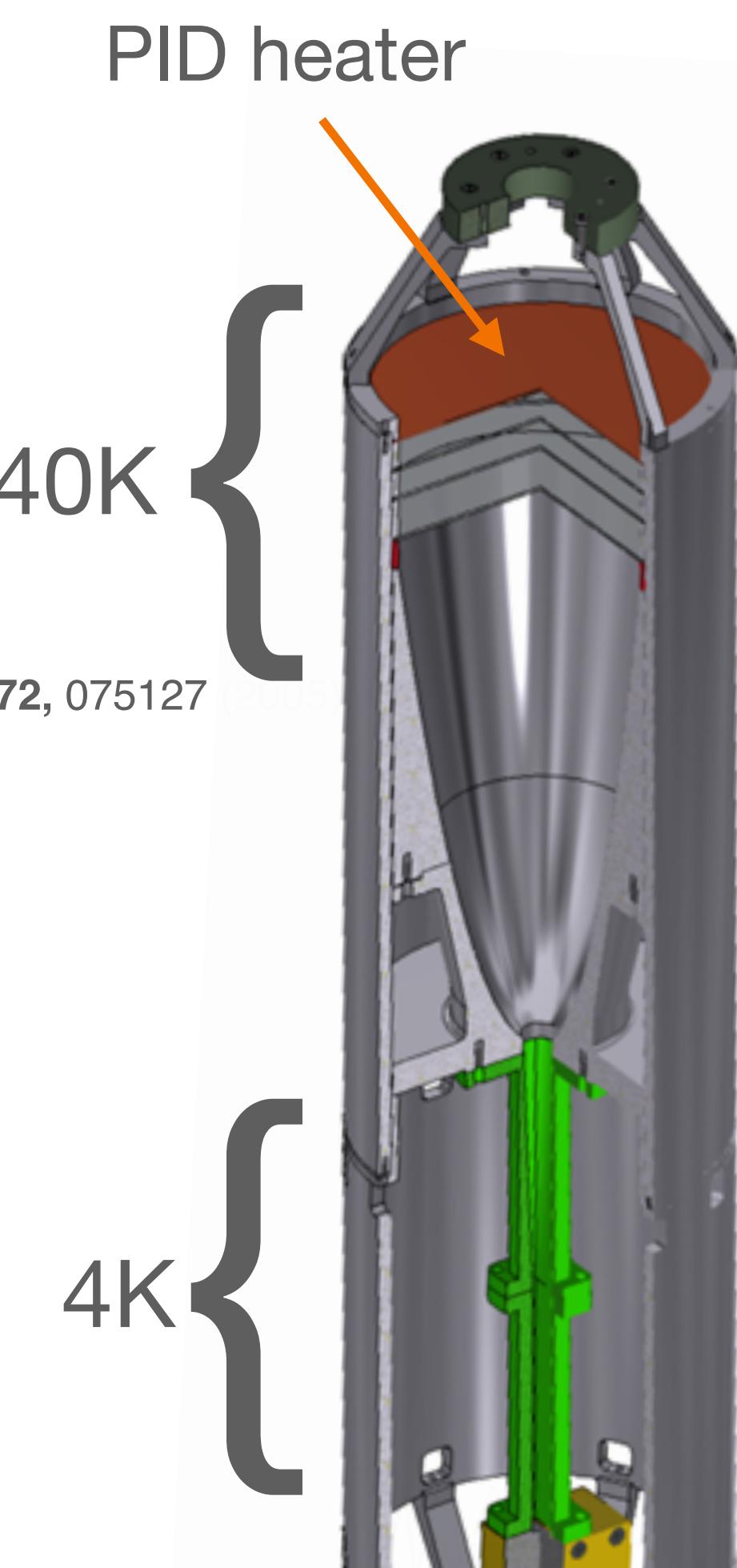
LHe bath cryostat

# Background noise

R. P. Meys, IEEE Trans. Microwave Theory Techn. 26, 34 (1978).

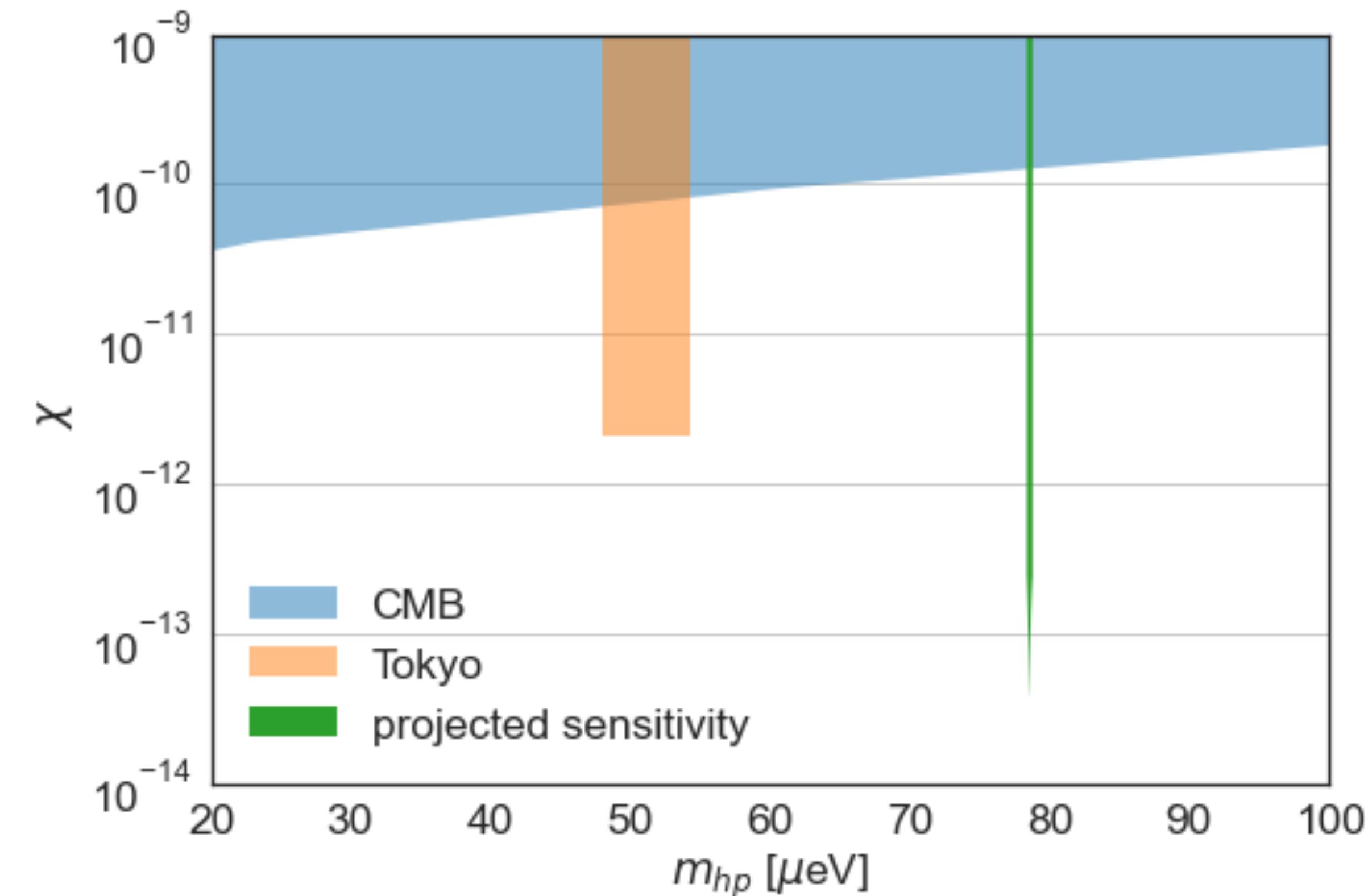


- Thermal noise can be enhanced if the mirror is heated.



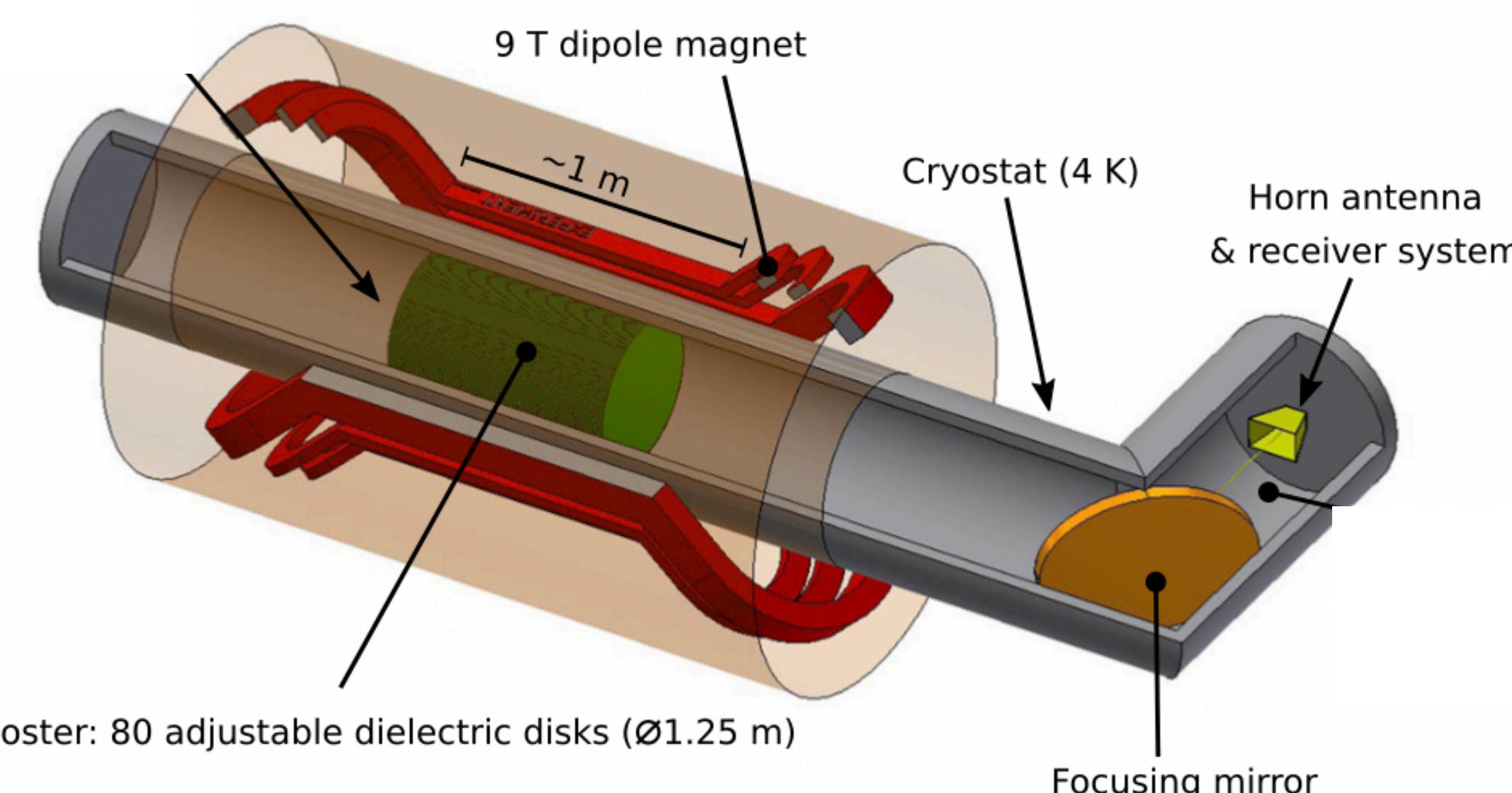
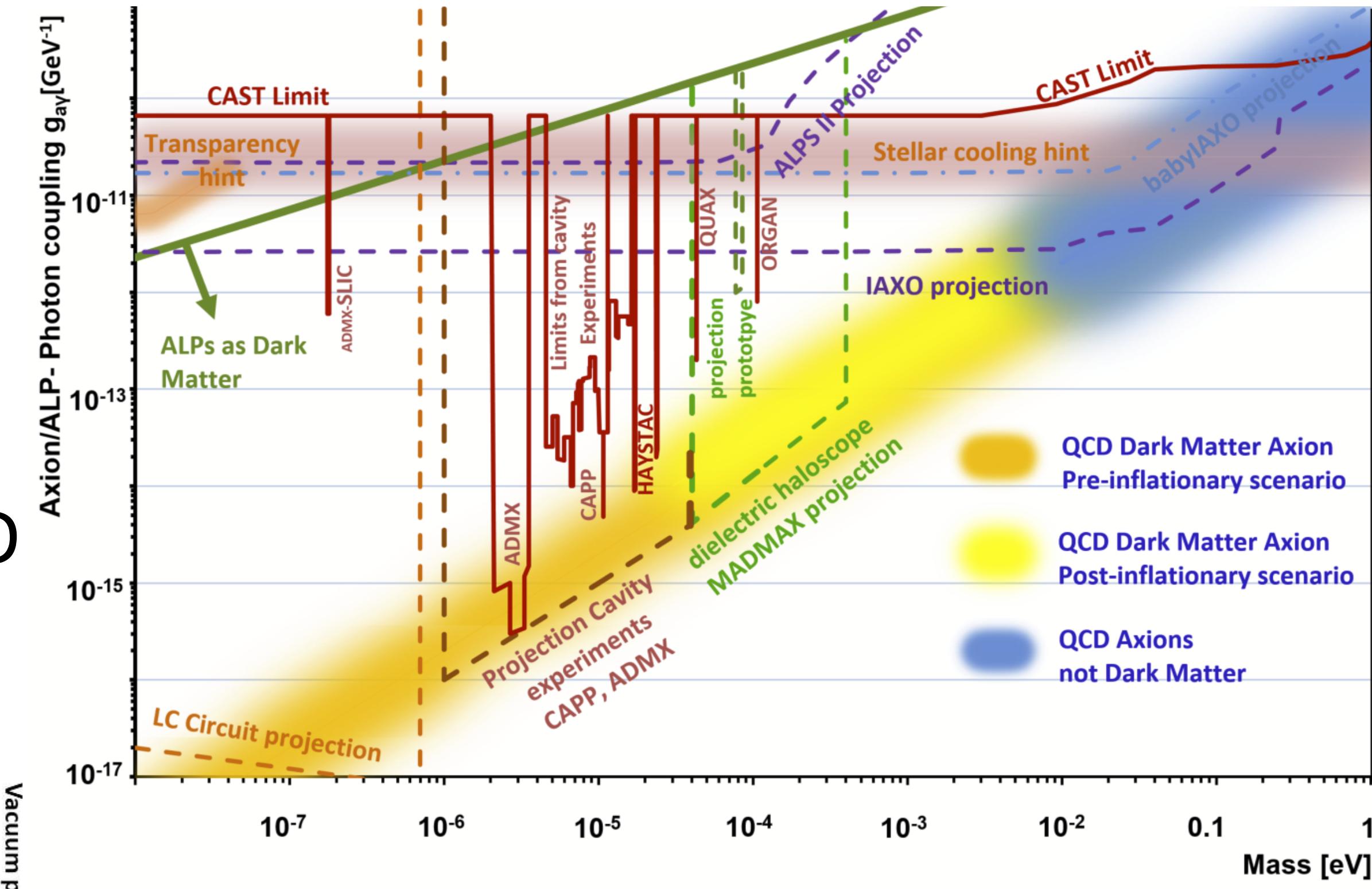
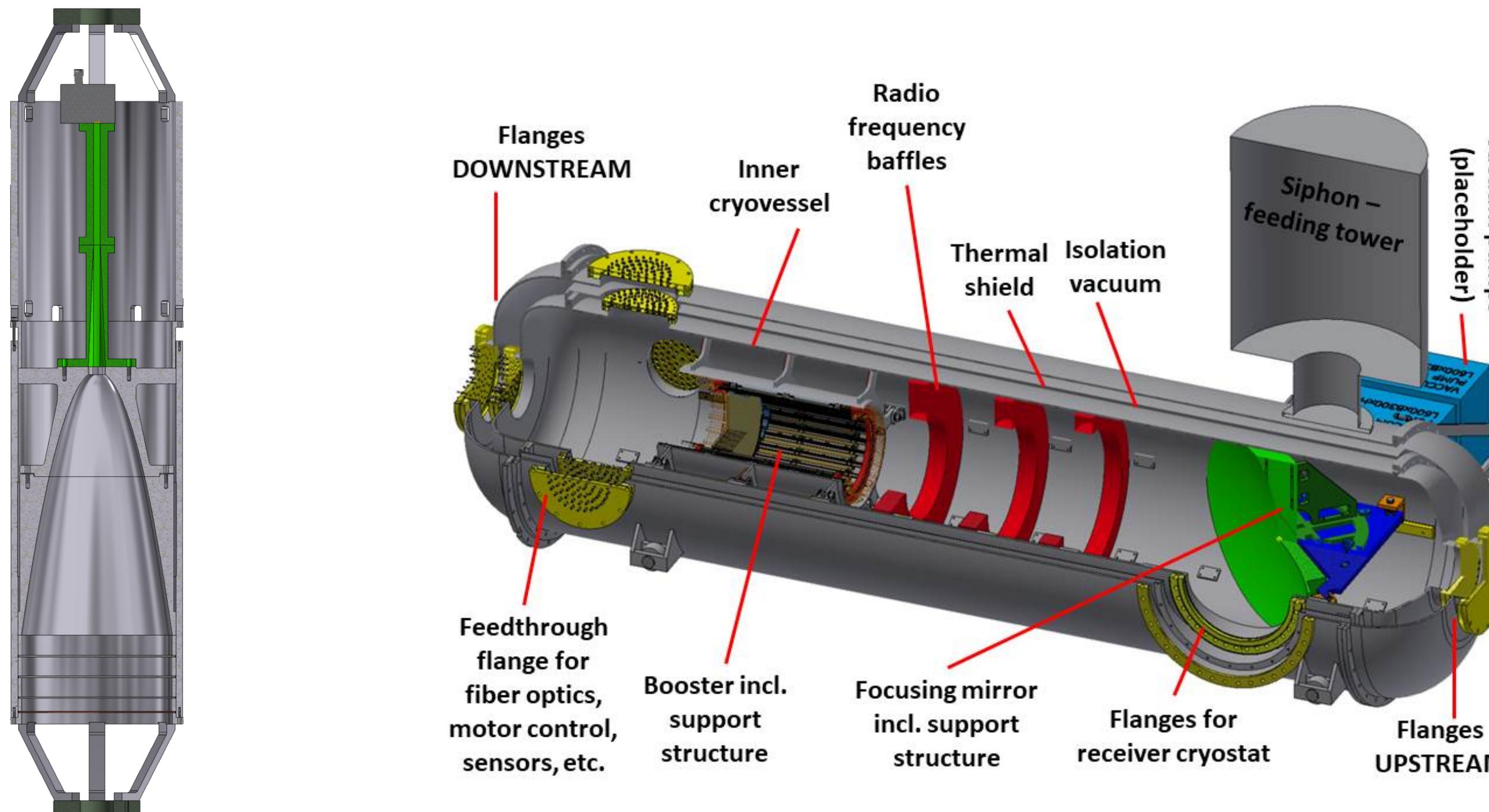
# Hidden photon search

- $\chi = 4.5 \times 10^{-9} \left( \frac{P_{\text{sens}}}{10^{-13} \text{ W}} \right)^{\frac{1}{2}} \left( \frac{1 \text{ m}^2}{A_{\text{mirror}}} \right)^{\frac{1}{2}} \left( \frac{1}{\beta^2} \right)^{\frac{1}{2}} \left( \frac{1}{\eta} \right)^{\frac{1}{2}} \left( \frac{0.45 \text{ GeV/cm}^3}{\rho_{\text{HPDM}}} \right)^{\frac{1}{2}}$
- 11K T<sub>sys</sub>, 7 days data taking,  
90% efficiency, S/N 5
- Δf ~ 20 MHz, χ ~ 1e-13



# Conclusion

- Dielectric haloscope is an ingenious approach to probe post-inflationary QCD axion dark matter

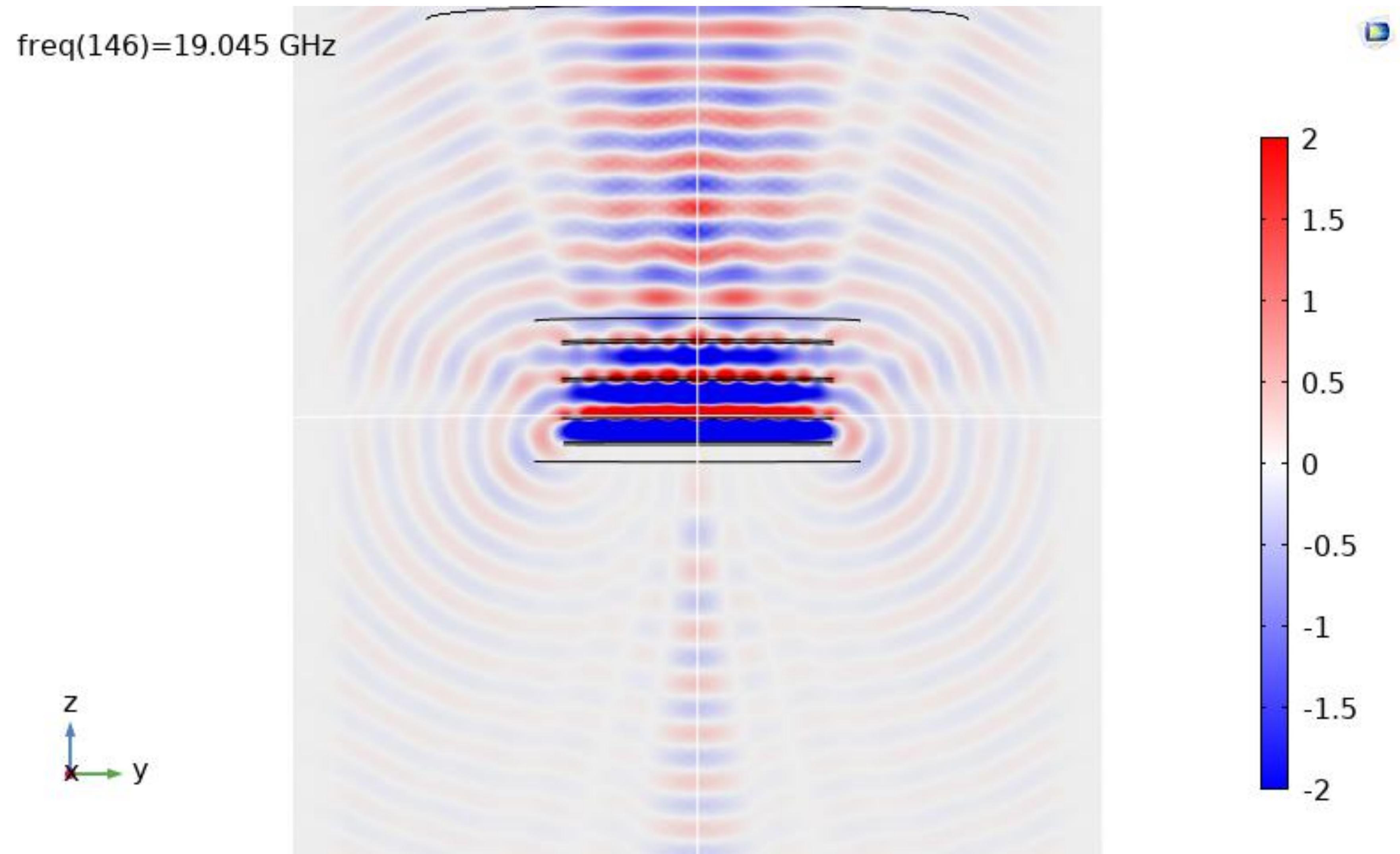




thank you  
Stay tuned!

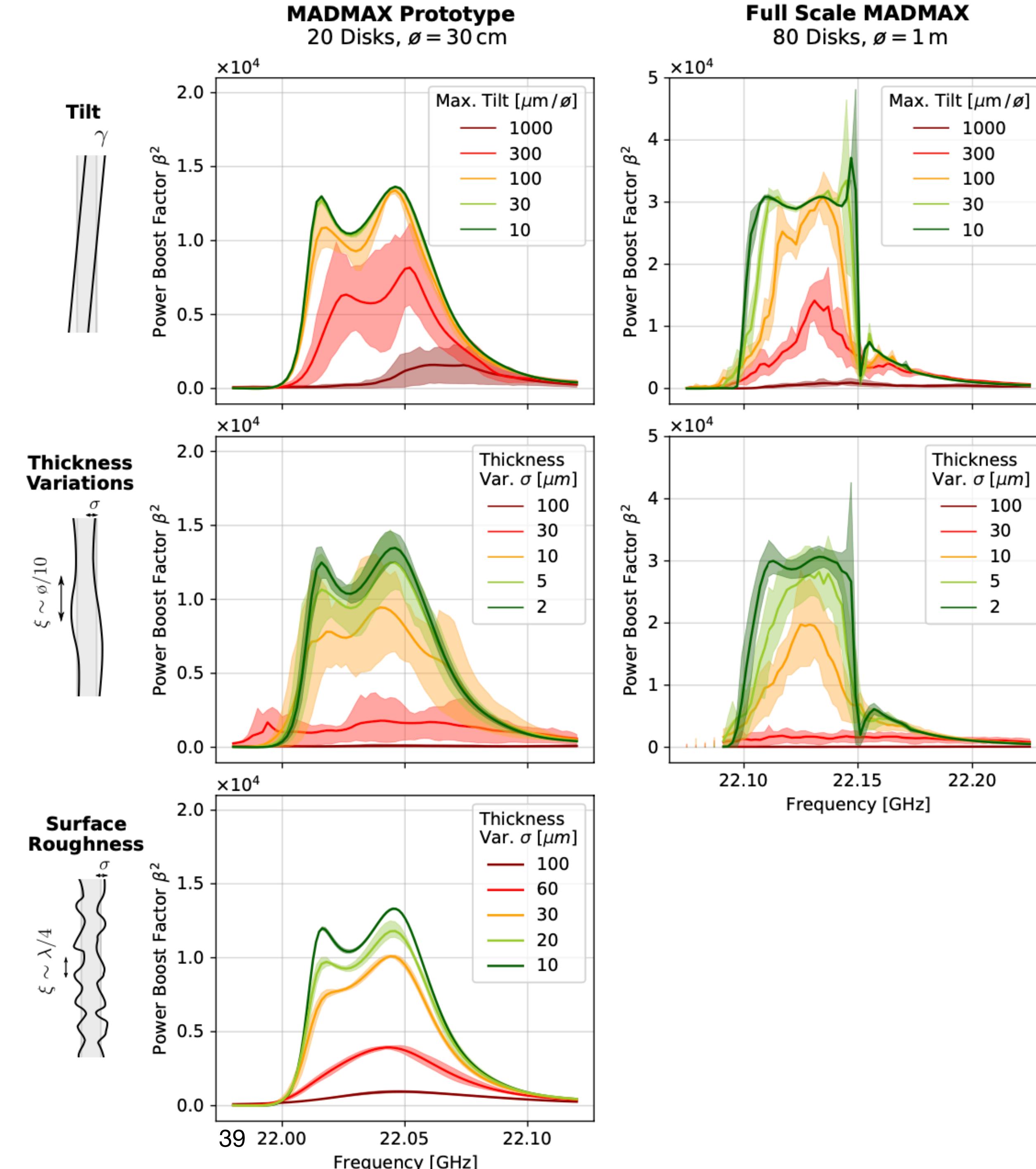
# Back-up

# Radiation from open booster

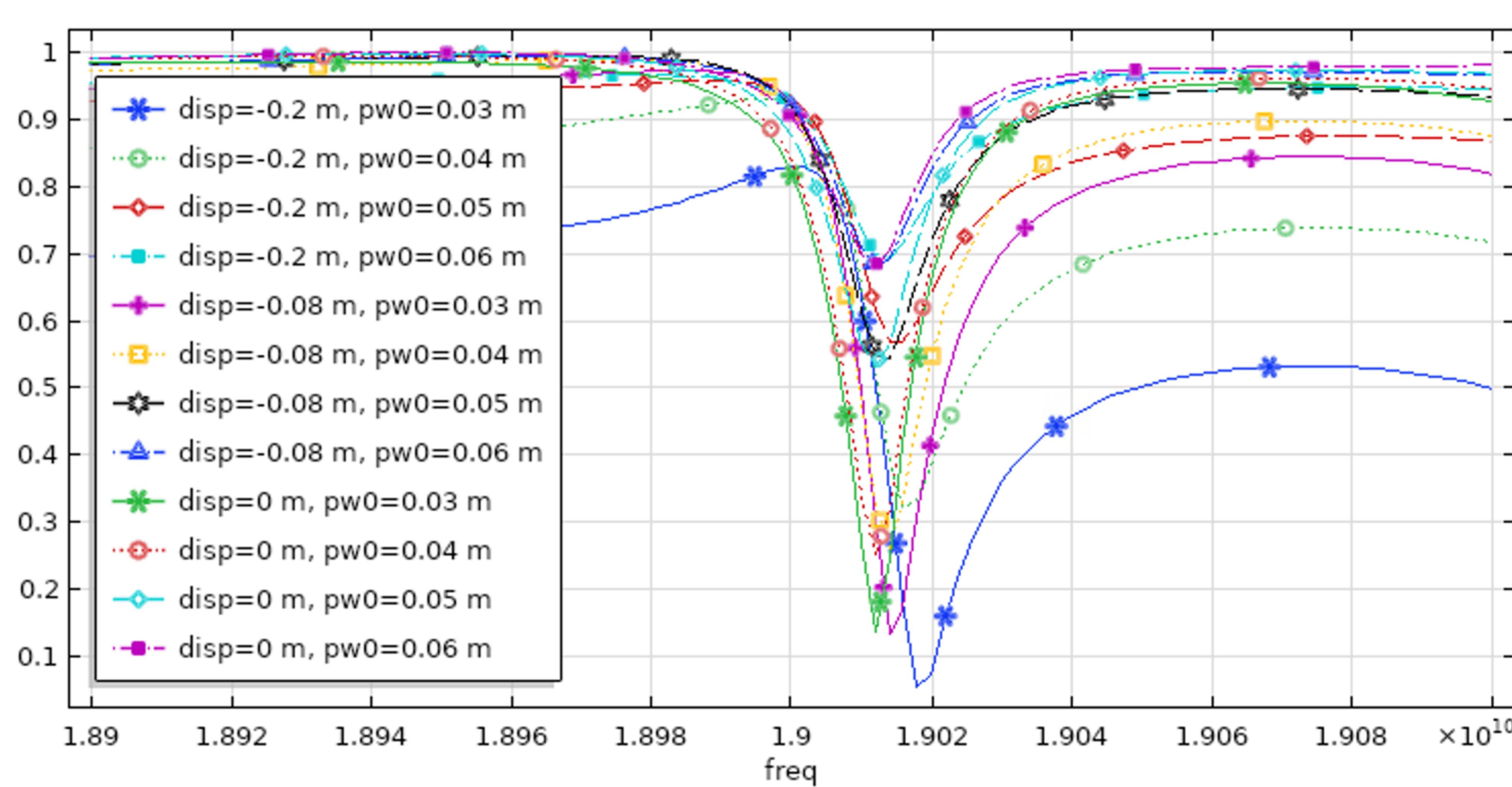


# Mechanical precision study

Simulation paper in preparation



# Reflectivity vs. beam waist for open system



# Transfer matrix formalism

A. J. Millar *et al.*, JCAP01 (2017) 061

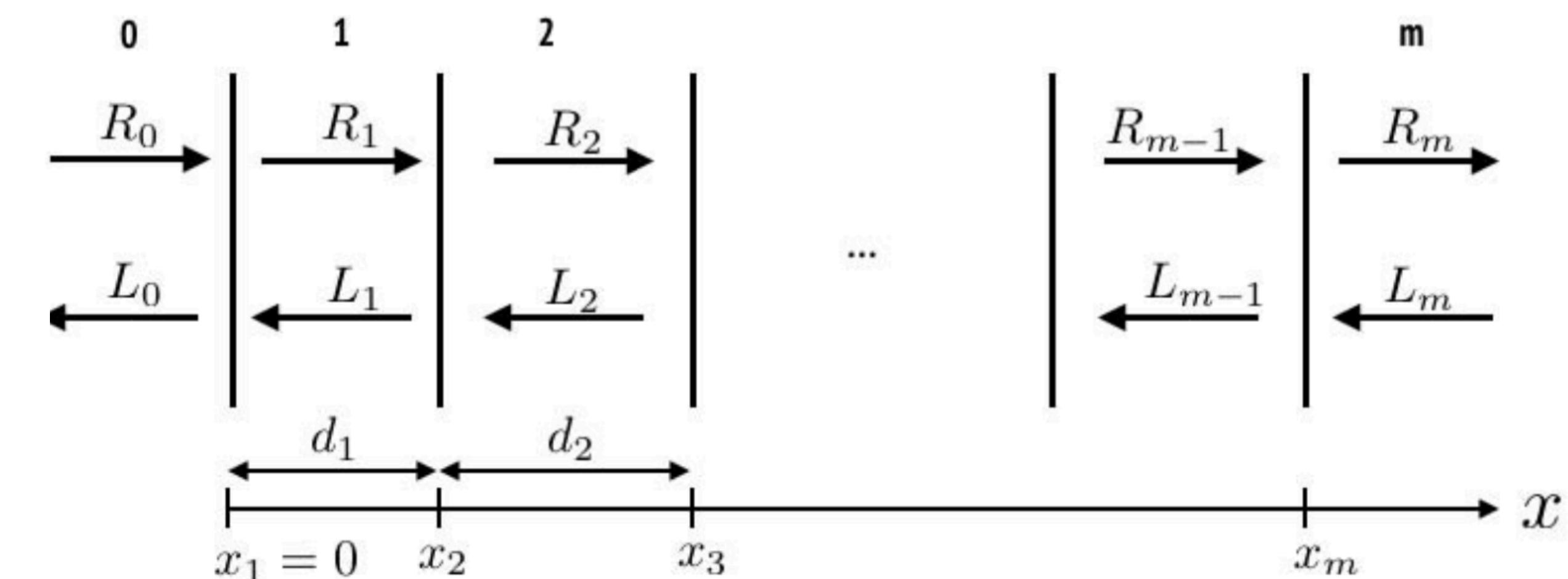
- Exact calculation of axion-induced traveling wave from give geometry

$$\begin{pmatrix} R_{r+1} \\ L_{r+1} \end{pmatrix} = G_r P_r \begin{pmatrix} R_r \\ L_r \end{pmatrix} + E_0 S_r \begin{pmatrix} 1 \\ 1 \end{pmatrix},$$

reflection  $G_r = \frac{1}{2n_{r+1}} \begin{pmatrix} n_{r+1}+n_r & n_{r+1}-n_r \\ n_{r+1}-n_r & n_{r+1}+n_r \end{pmatrix},$

propagation  $P_r = \begin{pmatrix} e^{+i\delta_r} & 0 \\ 0 & e^{-i\delta_r} \end{pmatrix},$

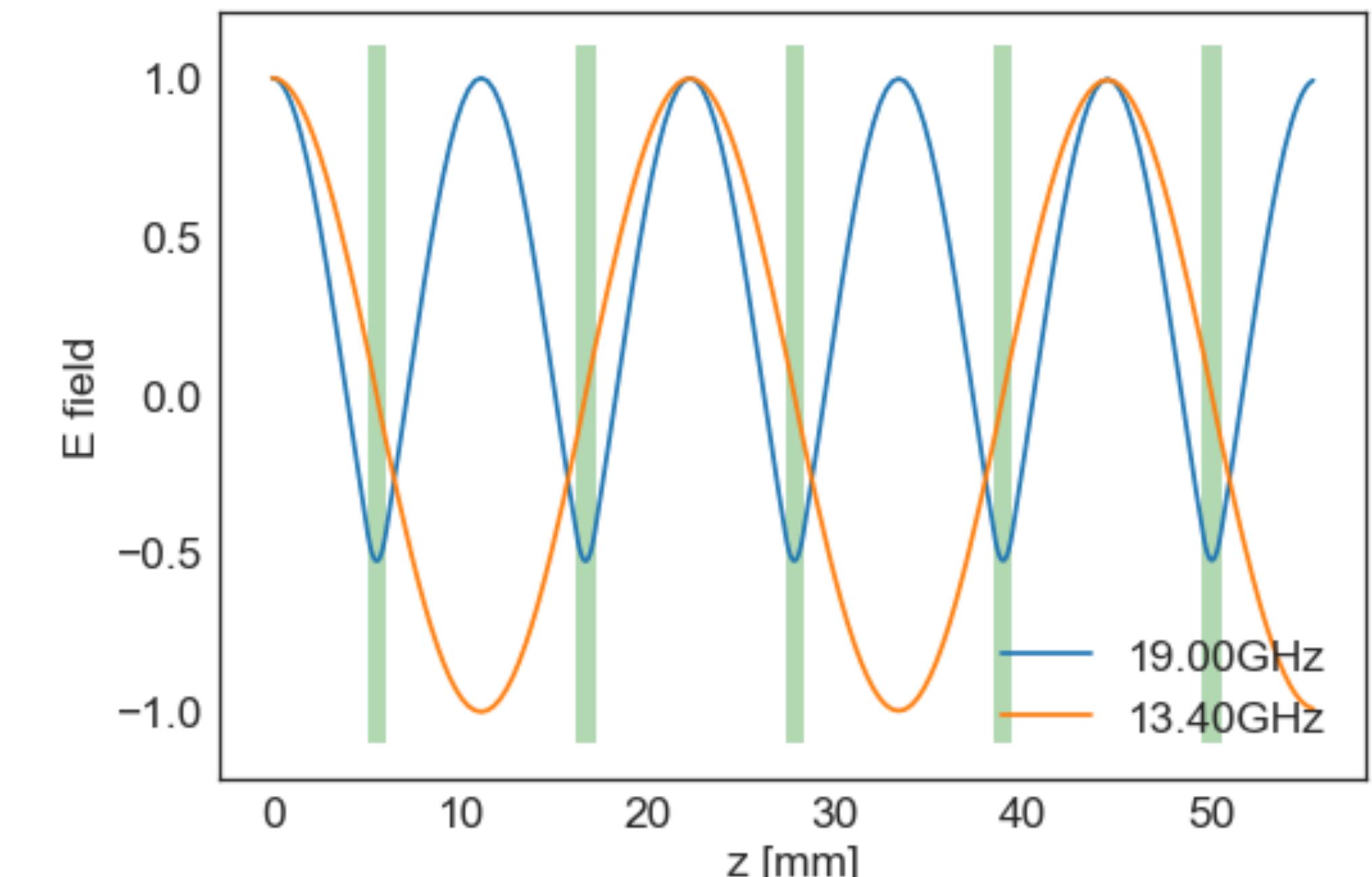
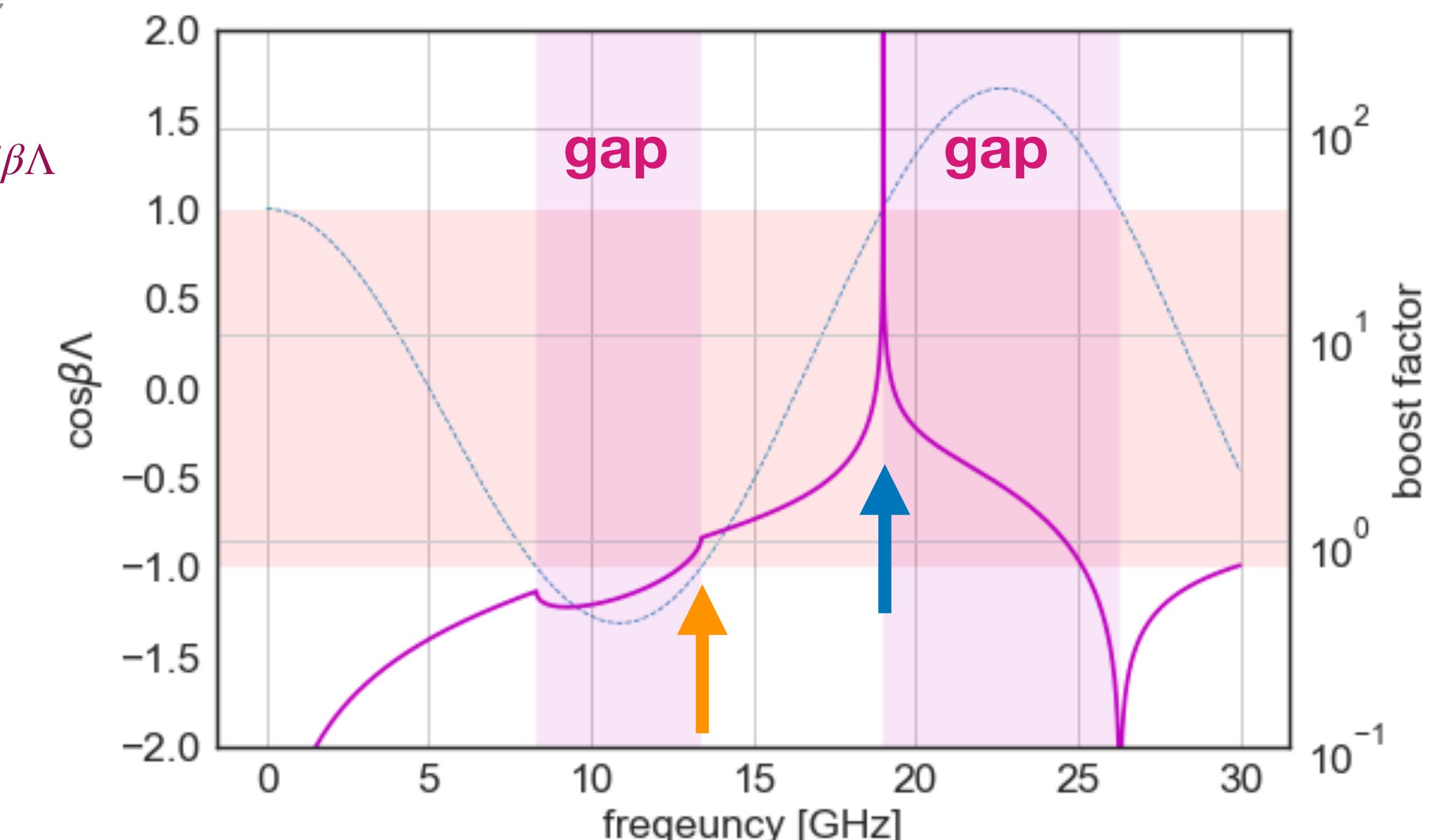
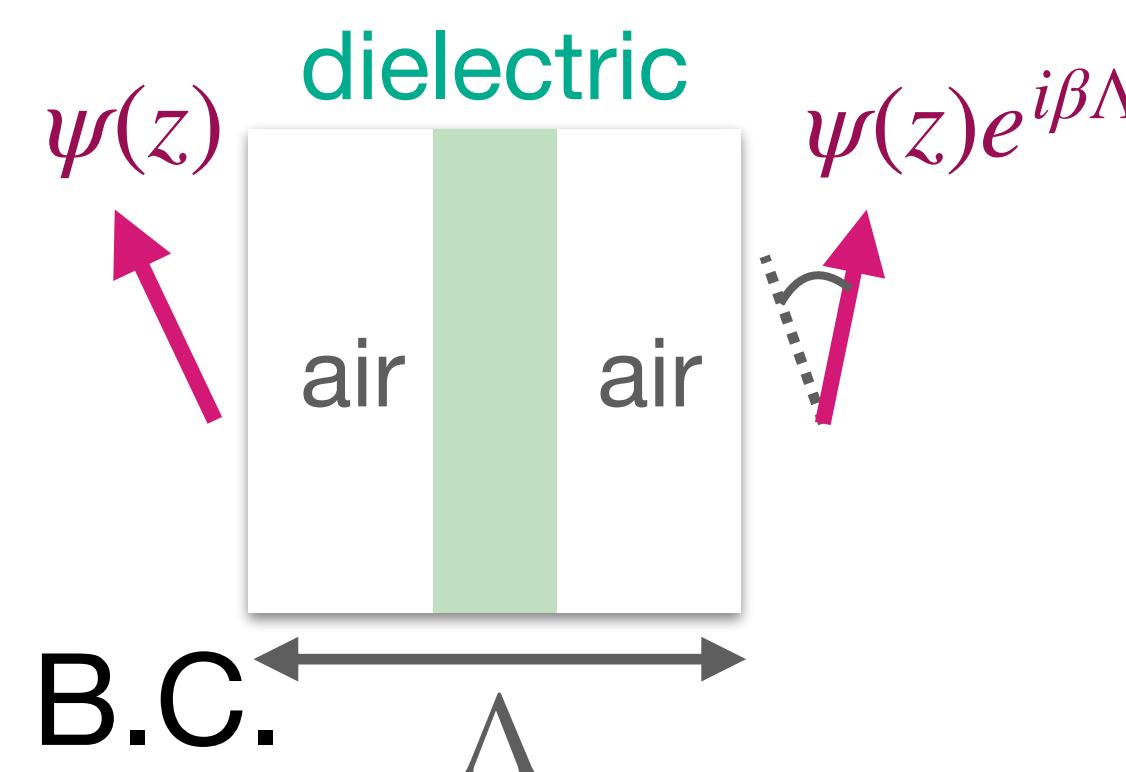
source  $S_r = \frac{A_{r+1} - A_r}{2} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}.$



# Disk spacing

## “infinite booster”

- Dispersion from Bloch B.C.
- “Band” structure
- Boost factor maximum  
@ the **boundary of 2<sup>nd</sup> pass/stop band**
  - Disk spacing for the boundary can be analytically calculated.
  - Bloch impedance ( $Z_B$ ): characteristic impedance of the periodic structure.

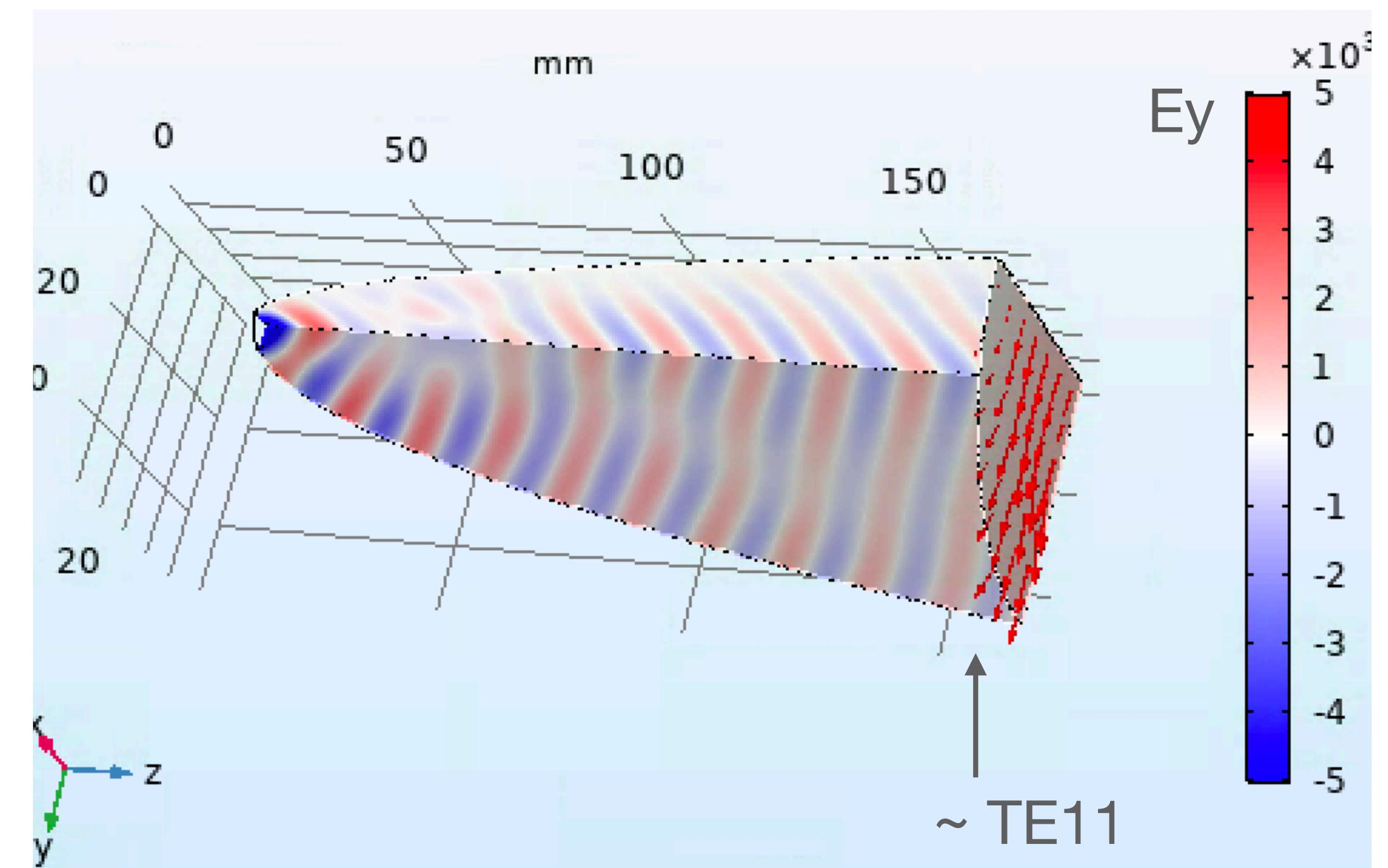
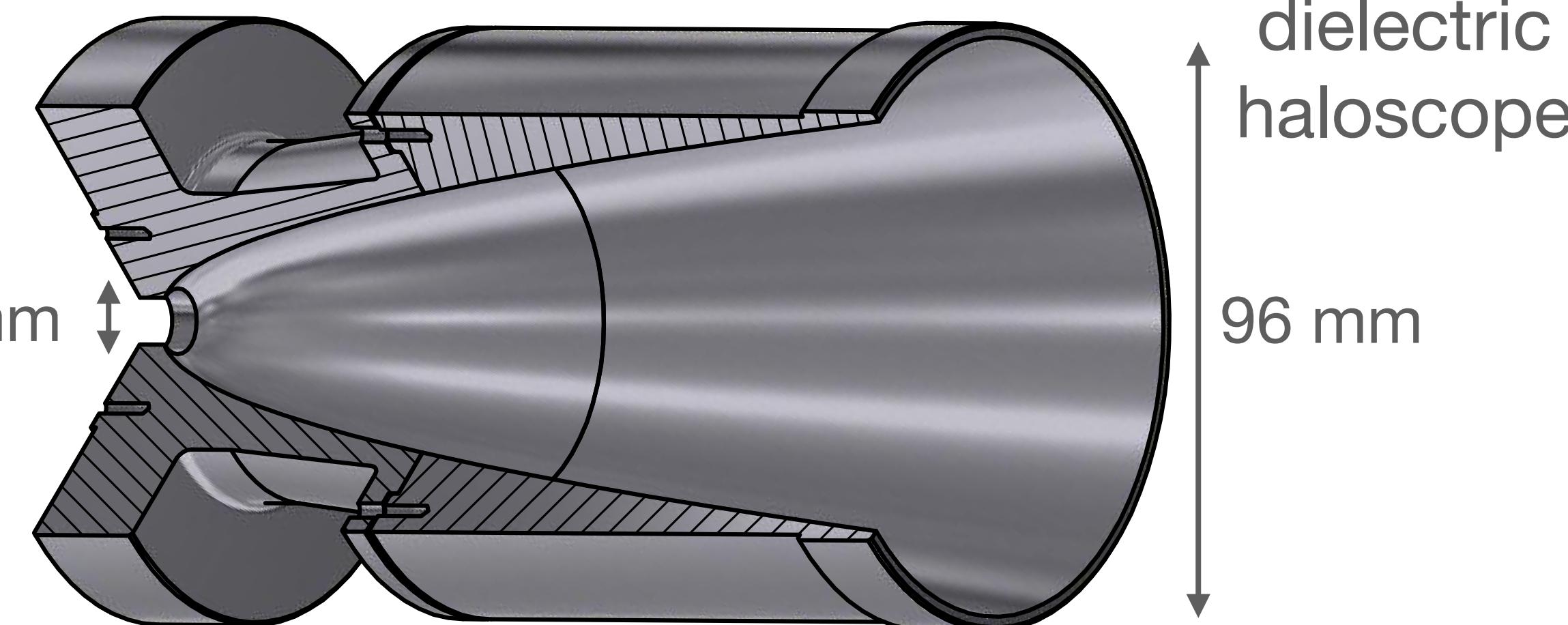


# Simulation parabolic taper

- “Matched” boundary
- $RL > 20\text{dB}$
- TE11 mode at the ports
- Additional gap btw. taper and booster.
- J. Diane, Int. J. Infrared Milli. Waves **5** (1984)

Receiver

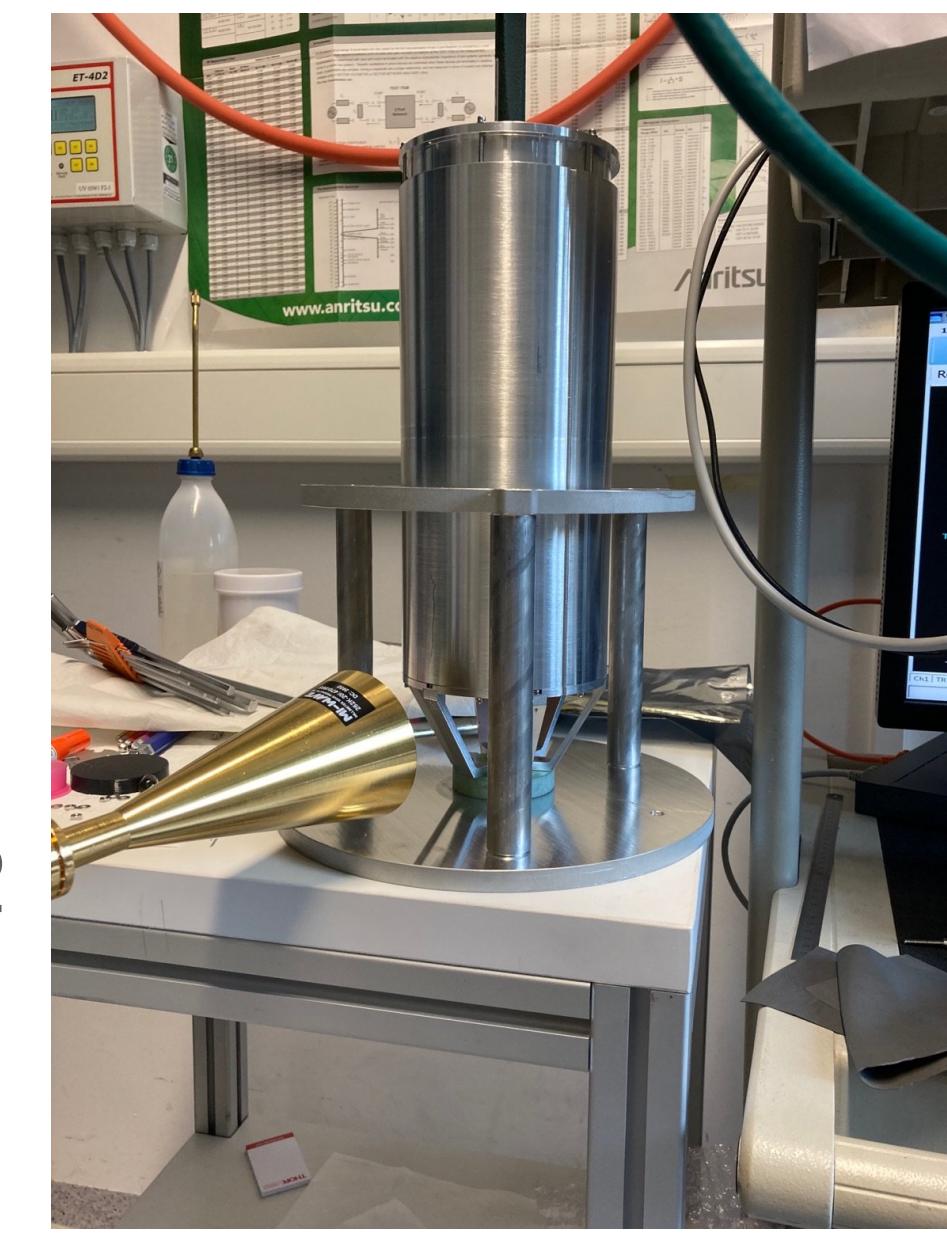
10.93 mm



# LOSS

- Simulation ~ 1dB vs. data > 6 dB
- Surface current leakage:  
solution: indium or EMI gasket
- Radiation leakage thru dielectric rims:  
solution: EMI gasket, metal sputtering

port 1



port 2

